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(71) Applicant:
 CANON KABUSHIKI KAISHA
 Ohta-ku Tokyo 146 (JP)

(72) Inventors:

- Le Dantec, Claude
35140 Saint Hilaire des Landes (FR)
- Piret, Philippe
35510 Cesson-Sevigne (FR)

(74) Representative:

Rinuy, Santarelli
 14, avenue de la Grande Armée,
 B.P. 237
 75822 Paris Cédex 17 (FR)

(54) Interleaver for turbo encoder

(57) The coding method to which the present invention relates takes into account:

- a predetermined integer M_1 , equal to or greater than 2,
- a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:
 - a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$, and
 - a number of binary data equal to the product of any integer number M and the integer N_0 , the smallest integer such that the polynomial $x^{N_0} + 1$ is divisible by each of the polynomials $g_i(x)$;
 - and includes a first operation of producing a number $K \cdot M_1$ of so-called "permuted" sequences, which each keep a divisibility by a polynomial $g_i(x)$

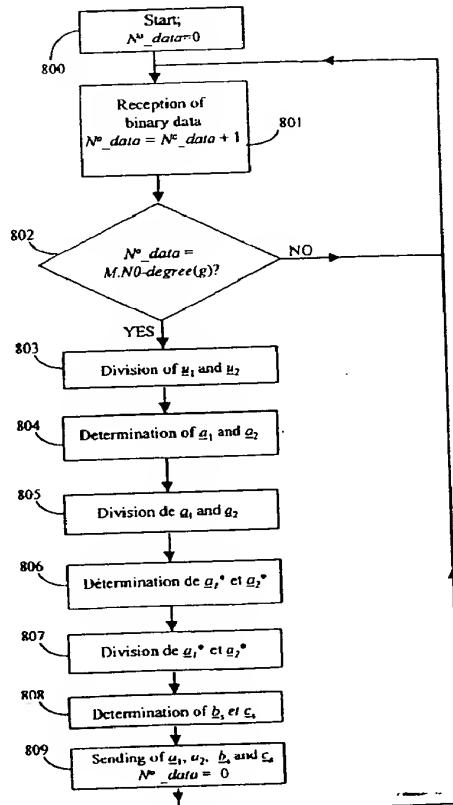


Fig. 8

Description

[0001] The present invention concerns a coding device, a coding method, a decoding device and method and systems implementing them.

5 [0002] It applies just as well to the coding of data representing a physical quantity, to the coding of data in the form of codes able to modulate a physical quantity, to the decoding of data modulated signals, and to the decoding of data representing a physical quantity. These data can for example represent images, sounds, computer data, electrical quantities or stored data.

10 [0003] The invention finds an application in the field of convolutional codes. When the latter are used to implement an iterative decoding, these codes are greatly improved when their coders contain a permutation device. In this case, they are normally referred to as "turbocodes" and the corresponding iterative decoder is referred to as a "turbodecoder".

[0004] On these subjects, documents which serve as a reference are, on the one hand, the article by Messrs. C. BERROU, A. GLAVIEUX and P. THITIMAJSIMA entitled "Near Shannon limit error-correcting coding and decoding: turbocodes" published with the reports of the conference "ICC'93", 1993, pages 1064 à 1070, and, on the other hand, 15 the article by Messrs. C. BERROU and A. GLAVIEUX entitled "Near Optimum error-correcting coding and decoding: turbo-codes" published by IEEE Transactions on Communication, Volume COM-44, pages 1261 to 1271, in October 1996.

20 [0005] However, the formation of permutation devices is far from being perfectly mastered. In general this device uses square or rectangular matrices in which one row after another is written and one column after another is read. These matrices are generally very large, for example of a size 256 x 256.

25 [0006] According to another method, in an article entitled "Weight distributions for turbo-codes using random and non-random permutations" published by Jet Propulsion Laboratory, with "TDA Progress Report", number 42-122, of 15 August 1995, Messrs. DOLINAR and DIVSALAR considered the permutations which, by numbering the k information positions between 0 and $k-1$, move the binary information placed at a position i to a position $e_i + f$, for "well chosen" values of e and f .

[0007] In this document, they give only one example where k is a power of 2. In addition, they do not discuss the possible reciprocal influence of the choice of the permutation device and of that of the elementary convolutional coders (2, 1) to be used to generate the coded sequences produced by the turbocoder (3, 1).

30 [0008] The evaluation of the corresponding turbocode consists of simulating its use on a transmission channel with different signal/noise ratio values and measuring the minimum value of this ratio for which a predetermined value of the probability of error on the binary values is reached.

[0009] However, the use of simulations as an evaluation tool can lead to a few problems.

35 [0010] For example, the permutation device with $k = 65536 = 256 \times 256$, mentioned above, is chosen, and a predetermined error probability equal to 10^{-5} is chosen to simulate the performance of a turbocode using this device. Consequently the mean number of errors on the binary values per block of 256×256 will be close to 1, but it will not be known whether each binary information item has the same error probability. This error probability could be fairly high for binary values having an "unlucky" position in the permutation device and this probability could be much smaller for more "lucky" positions.

40 [0011] A possible method for remedying this situation is to produce a harmonious and conjoint design of the permutation device and the two convolutional coders in order to guarantee a reasonable uniformity of the error rate on the binary values after decoding, as a function of the position of the binary information in the permutation device.

[0012] Another problem concerns the lack of algebraic tools for specifying the permutation devices. It will be useful to have available means for specifying a selection of permutation devices having a performance representative of the set of all the permutation devices.

45 [0013] The invention concerns principally the transmission of information represented by sequences of binary symbols:

$$\underline{u} = (u_0, u_1, \dots, u_{k-1}),$$

50 referred to as "sequences of information", which will be coded in a triplet of binary sequences,

$$\underline{v} = (a, b, c),$$

each of these sequences a , b and c being, by itself, representative of the sequence \underline{u} .

55 [0014] In the remainder of the description, in order to represent a sequence \underline{u} , the form $\bar{u} = (u_0, u_1, \dots, u_{k-1})$, is used indifferently along with the associated polynomial form:

$$u(x) = u_0 x^0 + u_1 x^1 + \dots + u_{k-1} x^{k-1}.$$

[0015] Equivalent notations will be used for the sequences \underline{a} , \underline{b} and \underline{c} . Using this second representation, it is known, in order to determine the triplet $\underline{v} = (\underline{a}, \underline{b}, \underline{c})$:

- to choose $a(x) = u(x)$;
- to choose $b(x) = u(x) \cdot h_1(x) / g(x)$,
where $g(x)$ is the polynomial, for example $g(x) = 1 + x + x^3$, corresponding, according to the representation in a sequence, to the sequence $(1, 1, 0, 1)$; and $h_1(x)$ is a polynomial, for example $h_1(x) = 1 + x + x^2 + x^3$, corresponding to the sequence $(1, 1, 1, 1)$; and
- by calling \underline{a}^* a sequence formed by permutation of the binary data of the sequence \underline{a} , to choose $c(x) = \underline{a}^*(x) \cdot h_2(x) / g(x)$
where $h_2(x)$ is a polynomial, for example $h_2(x) = (1 + x^2 + x^3)$ corresponding to the sequence $(1, 0, 1, 1)$.

[0016] Any choice of the polynomials $g(x)$, $h_1(x)$, $h_2(x)$ and of the permutation specifying the interlacer which associates the permuted sequence \underline{a}^* with the sequence \underline{a} , specifies a coder which will be referred to as a "turbocoder". All the sequences which a specified turbocoder can produce will be referred to as "turbocode".

[0017] In the remainder of the description, the term "first coder", will be given to the elementary recursive convolutional coder which produces the sequence \underline{b} and "second coder" will be given to the one which produces the sequence \underline{c} .

[0018] The polynomial divisions used are of the type consisting of division according to ascending powers, well known to persons skilled in the art. They use modulo 2 arithmetic. The sequences \underline{a} , \underline{b} and \underline{c} are binary sequences and in the general case the divisions which define \underline{b} and \underline{c} have a remainder.

[0019] This type of coding method has the advantage of lending itself to an iterative decoding which is powerful, relatively simple and inexpensive.

[0020] To implement it, several questions are posed.

25 I/ How to choose the polynomials $g(x)$, $h_1(x)$ et $h_2(x)$?
II/ How to choose the permutation of the terms of the sequence \underline{a} which produces the sequence \underline{a}^* ? Amongst the choices proposed, three examples of interlacers, that is to say of operators which permute the terms of the sequence \underline{a}^* , in order to form the sequence \underline{a}^* , are given below:

30 A) in the first example, after having arranged the terms of \underline{a} in a rectangular table, successively row by row and, for each row, from left to right, the sequence \underline{a}^* is formed by taking the terms in this table in succession column after column and, for each column, from top to bottom. For example, in the case of sequences of six terms and the use of a table of two rows of three columns, the interlacer transforms the sequence $\underline{a} = (a_0, a_1, a_2, a_3, a_4, a_5)$ into the sequence $\underline{a}^* = (a_0, a_3, a_1, a_4, a_2, a_5)$.
35 B) in a second example, the i -th term ($i = 0, 1, 2, \dots$) a_i^* of the sequence \underline{a}^* is chosen as being the term a_j of the sequence \underline{a} , with $j = s \cdot i + t$ calculated modulo the number of terms in the sequence \underline{a} , s and t being integers. For example, if the number of terms of the sequence \underline{a} is six and if $s = 5$ and $t = 3$, the interlacer transforms the sequence $\underline{a} = (a_0, a_1, a_2, a_3, a_4, a_5)$ into the sequence $\underline{a}^* = (a_3, a_2, a_1, a_0, a_5, a_4)$.
40 C) in the third example, the permutation chosen is random.

III/ How to avoid the division defining $b(x)$ not having a remainder? and

IV/ How to avoid the division defining $c(x)$ having a remainder?

45 [0021] Responding to these last two questions amounts to resolving a problem frequently mentioned in the literature on turbocodes, which is that of the "return to the zero state" of the elementary convolutional coders defining \underline{b} and \underline{c} . Since the turbocoders have two elementary recursive coders, the second of which uses a permutation \underline{a}^* of the sequence \underline{a} , it is wished to guarantee that the polynomials $a(x)$ and $a^*(x)$ representing the information sequence $u(x)$ are simultaneously divisible by $g(x)$. Ensuring this divisibility condition for $a(x)$ is simple since it suffices to construct $a(x)$ from $u(x)$ whilst supplementing $u(x)$ with padding symbols in a number equal to the degree of $g(x)$ and whose only function is to guarantee the absence of a remainder in the division serving to produce $b(x)$ from $a(x)$.
50 [0022] Choosing a permutation producing $a^*(x)$ from $a(x)$ which guarantees both the divisibility of $a^*(x)$ by $g(x)$ and good error correction performances for the turbocode thus specified is, on the other hand, more difficult.
55 [0023] This problem can give rise to disparities between the probabilities of errors after decoding of the different bits constituting $u(x)$.
[0024] In an article which appeared in volume 31 No 1 of the journal "Electronics Letters" of 5 January 1995, Messrs. BARBULESCU and PIETROBON disclosed that an interlacer can be described by successively and cyclically arranging the terms of the sequence \underline{a} in a number of sequences equal to the degree of the polynomial $g(x)$ incremented by

one, and that, in such case, permutations internal to each of the sequences thus formed give rise to equality between remainder of the division defining the sequence \underline{b} and that of the division defining the sequence \underline{c} .

[0025] However, and contrary to what is stated in this article, this statement is true only if the polynomial $g(x)$ is of the form $\sum_{i=0 \text{ to } m} x^i$.

5 [0026] In an article entitled "Turbo-block-codes", published with the reports of the seminar "Turbo Coding" organised by the Institute of Technology of Lund (Sweden) (Department of Applied Electronics) in August 1996, Messrs C. BER-
ROU, S. EVANO and G. BATTAIL disclosed that, by arranging the terms of the sequence \underline{u} cyclically, in a number of columns equal to a multiple of the degree $N0$ of the polynomial of type $x^n - 1$ of the lowest strictly positive degree which is divisible by $g(x)$, permutations internal to each of the columns thus formed mean that the sum of the remainder of the division defining the sequence \underline{b} and of that of the division defining the sequence \underline{c} is nil, so that the concatenation of the sequences is divisible by g .

10 [0027] This document, just like the previous one, therefore restricts the choice of the interlacers to particular forms working independently on sub-sets of the terms of the sequence \underline{a} by applying internal permutations to them. It does not however guarantee that individually $a(x)$ and $a^*(x)$ are divisible by $g(x)$. The only thing that is guaranteed is the divisibility by $g(x)$ of the polynomial representing the concatenation $(\underline{a}, \underline{a}^*)$, consisting of putting the two sequences \underline{a} and \underline{a}^* end to end.

[0028] There results a possible loss of efficacy of the decoder since the latter is not informed of the state which the coder had at the moment marking the end of the calculation of \underline{b} and the start of the calculation of \underline{c} .

15 [0029] None of the articles cited proposes an effective choice of interlacer.

[0030] The present invention sets out to remedy these drawbacks by proposing on the one hand families of interlacers which guarantee return to zero at the end of the sequence \underline{c} , when the sequence \underline{b} returns to zero, and on the other hand proposing a choice of interlacers which is wider than that proposed by the articles cited above.

[0031] To this end, according to a first aspect, the present invention relates to a coding method characterised in that:

25 1/ it takes into account:

- a predetermined integer $M1$, equal to or greater than 2,
- a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:
 - a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$, and
 - a number of binary data equal to the product of any integer number M and the integer $N0$, the smallest integer such that the polynomial $x^{N0} + 1$ is divisible by each of the polynomials $g_i(x)$;

30 25 2/ it includes a first operation of producing a number $K * M1$ of so-called "permuted" sequences a_{ij}^* , ($i=1, \dots, K$; $j=1, \dots, M1$), each sequence a_{ij}^* :

- being obtained by a permutation of the corresponding sequence a_i , said permutation being, in a representation where the binary data of each sequence a_i are written, row by row, in a table with $N0$ columns and M rows, the resultant of any number of so-called elementary permutations which, each:
 - either has the property of transforming the cyclic code of length $N0$ and with a generator polynomial $g_i(x)$ into an equivalent cyclic code with a generator polynomial $g_{ij}(x)$ which can be equal to $g_i(x)$, and acts by permutation on the $N0$ columns of the table representing a_i ,
 - or is any permutation of the symbols of a column of said table; and
- having, in consequence, a polynomial representation $a_{ij}^*(x)$ which is equal to a polynomial product $c_{ij}(x)g_{ij}(x)$,
- at least one permuted sequence a_{ij}^* being different from the corresponding sequence a_i ,

40 45 50 3/ it includes a second operation of producing $M1$ redundant sequences whose polynomial representation is equal to $\sum f_{ij}(x) c_{ij}(x)$, for $j=1, \dots, M1$, each polynomial $f_{ij}(x)$ being a polynomial with a degree at most equal to the degree of the polynomial $g_{ij}(x)$ with the same indices i and j .

55 [0032] There have been introduced above, in a representation where the binary data of the sequence \underline{a} are classified in a table of $N0$ columns and M rows, the successions of permutations taken from all the permutations including, on the one hand, the automorphisms of the binary cyclic code of length $N0$ and with a generator polynomial $g(x)$, permuting with each other at least two of the $N0$ columns of the table and, on the other hand, the permutations working solely on data in the same column and permuting with each other at least two of the said data.

[0033] The inventors have discovered that all these successions of permutations, and only these, guarantee that, for any polynomial $a(x)$ whose division by $g(x)$ leaves a nil remainder, the permuted polynomial $a'(x)$ has the same property.

[0034] For a study of the conditions governing the choice of g_{ij} , the reader can refer to page 234 of the book by Mrs F.J. MACWILLIAMS and Mr N.J.A. SLOANE "The theory of error-correcting codes" published by North-Holland in 1977 and whose seventh impression was printed in 1992.

[0035] All the choices described in the present invention include the interlacers disclosed in the two articles mentioned above. Thus the performance expressed in terms of error rate as a function of the signal/noise ratio can be improved without increasing the complexity of the turbocoder or that of the turbodecoder.

[0036] According to a second aspect, the present invention relates to a decoding method characterised in that:

1/ it takes into account:

- a predetermined integer M_1 , equal to or greater than 2,
- a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:
 - a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$ and has no multiple polynomial factors, and
 - a number of binary data equal to the product of any odd integer number M and the integer N_0 , the smallest integer such that the polynomial $x^{N_0}+1$ is divisible by each of the polynomials $g_i(x)$;

2/ it includes a first operation of producing a number $K \cdot M_1$ of so-called "permuted", sequences a_{ij}^* , ($i=1, \dots, K$; $j=1, \dots, M_1$), each sequence a_{ij}^* having a polynomial representation equal to $a_{ij}^*(x) = a_i(x^{e_{ij}})$ modulo (x^n+1) , where

- n is the product of the number M and the integer N_0 ,
- e_{ij} is a relatively prime number with n
- c_{ij} is the quotient of $a_{ij}^*(x)$ by $g_{ij}(x)$,
- the polynomial $g_{ij}(x)$ is the generator polynomial of the smallest cyclic code of length N_0 containing the polynomial $g_i(x^{e_{ij}})$ modulo $(x^{N_0}+1)$,
- at least one permuted sequence a_{ij}^* being different from the corresponding sequence a_i :

3/ it includes a second operation of producing M_1 redundant sequences whose polynomial representation is equal to $\sum f_{ij}(x) c_{ij}(x)$, for $j=1, \dots, M_1$, each polynomial $f_{ij}(x)$ being a predetermined polynomial with a degree at least equal to the degree of the polynomial $g_{ij}(x)$ with the same indices i and j .

[0037] It should be noted here that it is then stated that e belongs to the cycle of 2, modulo $M \cdot N_0$.

[0038] By virtue of these provisions, on the one hand the majority of the columns in the table can be moved by permutation, and on the other hand, in this restricted choice, the minimum distance of the turbocode is more easily analysable and can therefore be optimised.

[0039] This second aspect of the invention has the same advantages as the first aspect.

[0040] The inventors observed that implementing the method of the present invention, in each of its aspects, as disclosed above, has the advantage that any error estimation by the corresponding decoder converges. The case where the error estimation does not converge is therefore excluded by the implementation of the present invention.

[0041] According to particular characteristics, during the first production operation, all the values of the exponents e_{ij} having same value of the index j are identical.

[0042] By virtue of these provisions, the coding method to which the present invention relates makes it possible to effect all the interlacings to j fixed in the same way. It is therefore simple to implement.

[0043] According to particular characteristics, during the first production operation, all the values of the exponents e_{ij} are equal to a power of 2.

[0044] By virtue of this provision, the polynomials g_{ij} are all identical.

[0045] According to particular characteristics, the coding method to which the present invention relates, as briefly disclosed above, includes an operation of transmitting on the one hand sequences a_i , and, on the other hand, a sub-set of the data of the other sequences.

[0046] By virtue of these provisions, the efficiency of the method is increased

[0047] According to a third aspect, the present invention relates to a coding device characterised in that it includes a processing means adapted to:

1/ take into account:

- a predetermined integer M_1 , equal to or greater than 2,
- a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:
 - a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$, and
 - a number of binary data equal to the product of any integer number M and the integer N_0 , the smallest integer such that the polynomial $x^{N_0}+1$ is divisible by each of the polynomials $g_i(x)$;

10 2/ production of a number $K \cdot M_1$ of so-called "permuted" sequences, a_{ij}^* , ($i=1, \dots, K$; $j=1, \dots, M_1$), each sequence a_{ij}^*

- being obtained by a permutation of the corresponding sequence, said permutation being, in a representation where the binary data of each sequence a_i are written, row by row, in a table with N_0 columns and M rows, the resultant of any number of so-called elementary permutations which, each:
 - either has the property of transforming the cyclic code of length N_0 and with a generator polynomial $g_i(x)$ into an equivalent cyclic code with a generator polynomial $g_{ij}(x)$ which can be equal to $g_i(x)$, and acts by permutation on the N_0 columns of the table representing a_i ,
 - or is any permutation of the symbols of a column of said table; and
- having, in consequence, a polynomial representation $a_{ij}^*(x)$ which is equal to a polynomial product $c_{ij}(x)g_{ij}(x)$,
- at least one permuted sequence a_{ij}^* being different from the corresponding sequence a_i ,

25 3/ producing M_1 redundant sequences whose polynomial representation is equal to $\sum f_{ij}(x) c_{ij}(x)$, for $j=1, \dots, M_1$, each polynomial $f_{ij}(x)$ being a polynomial with a degree at least equal to the degree of the polynomial $g_{ij}(x)$ with the same indices i and j .

30 [0048] According to a fourth aspect, the present invention relates to a coding device characterised in that it has a processing means adapted to:

1/ take into account:

- a predetermined integer M_1 , equal to or greater than 2,
- a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:
 - a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$ and has no multiple polynomial factors, and
 - a number of binary data equal to the product of any odd integer number M and the integer N_0 , the smallest integer such that the polynomial $x^{N_0}+1$ is divisible by each of the polynomials $g_i(x)$;

40 2/ produce a number $K \cdot M_1$ of so-called "permuted" sequences a_{ij}^* , ($i=1, \dots, K$; $j=1, \dots, M_1$), each sequence a_{ij}^* having a polynomial representation equal to $a_{ij}^*(x) = a_i^*(x^{e_{ij}}) \bmod (x^n+1)$, where

- n is the product of the number M and the integer N_0 ,
- e_{ij} is a relatively prime number with n
- c_{ij} is the quotient of $a_{ij}^*(x)$ by $g_{ij}(x)$,
- the polynomial $g_{ij}(x)$ is the generator polynomial of the smallest cyclic code of length N_0 containing the polynomial $g_i(x^{e_{ij}}) \bmod (x^{N_0}+1)$,
- at least one permuted sequence a_{ij}^* being different from the corresponding sequence a_i ;

45 3/ produce M_1 redundant sequences whose polynomial representation is equal to $\sum f_{ij}(x) c_{ij}(x)$, for $j=1, \dots, M_1$, each polynomial $f_{ij}(x)$ being a predetermined polynomial with a degree at least equal to the degree of the polynomial $g_{ij}(x)$ with the same indices i and j .

55 [0049] According to a fifth aspect, the present invention relates to a decoding method characterised in that:

1/ it takes into account:

- a predetermined integer $M1$, equal to or greater than 2,
- a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:
 - a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$, and
 - a number of binary data equal to the product of any integer number M and the integer $N0$, the smallest integer such that the polynomial $x^{N0}+1$ is divisible by each of the polynomials $g_i(x)$;

10 2/ it includes an operation of parallel turbodecoding of K sequences of symbols using the divisor polynomials $g_{ij}(x)$.

3/ it includes, for each a_i , $M1$ permutation operations, at least one of which is not identity, each permutation being, in a representation where the binary data of each sequence a_i are written, row by row, in a table with $N0$ columns and M rows, the resultant of any number of so-called elementary permutations which, each:

- either has the property of transforming the cyclic code of length $N0$ and with a generator polynomial $g_i(x)$ into an equivalent cyclic code with a generator polynomial $g_{ij}(x)$ which can be equal to $g_i(x)$, and acts by permutation on the $N0$ columns of the table representing a_i ,
- or is any permutation of the symbols of a column of said table.

20 [0050] According to a sixth aspect, the present invention relates to a decoding method characterised in that:

1/ it takes into account:

- a predetermined integer $M1$, equal to or greater than 2,
- a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:
 - a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$ and which has no multiple polynomial factors, and
 - a number of binary data equal to the product of any odd integer number M and the integer $N0$, the smallest integer such that the polynomial $x^{N0}+1$ is divisible by each of the polynomials $g_i(x)$;

25 2/ it includes an operation of parallel turbodecoding of K sequences of symbols using the divisor polynomials $g_{ij}(x)$.

30 3/ the said parallel turbodecoding operation including a permutation operation producing so-called "permuted" sequences, a_{ij}^* ($i=1, \dots, K$; $j=1, \dots, M1$), each permuted sequence a_{ij}^* having a polynomial representation equal to $a_{ij}^*(x)=a_i^*(x^{e_{ij}})$ modulo (x^n+1) , where:

- n is the product of the number M and the integer $N0$,
- e_{ij} is a relatively prime number with n
- c_{ij} is the quotient of $a_{ij}^*(x)$ by $g_{ij}(x)$,
- the polynomial $g_{ij}(x)$ is the generator polynomial of the smallest cyclic code of length $N0$ containing the polynomial $g_i(x^{e_{ij}})$ modulo $(x^{N0}+1)$,
- at least one permuted sequence being different from the corresponding sequence a_i .

40 45 [0051] According to a seventh aspect, the present invention relates to a decoding device characterised in that it includes a processing means adapted:

1/ to take into account:

- a predetermined integer $M1$, equal to or greater than 2,
- a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:
 - a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$, and
 - a number of binary data equal to the product of any integer number M and the integer $N0$, the smallest integer such that the polynomial $x^{N0}+1$ is divisible by each of the polynomials $g_i(x)$;

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2/ to perform an operation of parallel turbodecoding of K sequences of symbols using the divisor polynomials $g_{ij}(x)$.
3/ to perform, for each a_i , $M1$ permutation operations, at least one of which is not identity, each permutation being, in a representation where the binary data of each sequence a_i are written, row by row, in a table with $N0$ columns and M rows, the resultant of any number of so-called elementary permutations which, each:

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- either has the property of transforming the cyclic code of length $N0$ and with a generator polynomial $g_i(x)$ into an equivalent cyclic code with a generator polynomial $g_{ij}(x)$ which can be equal to $g_i(x)$, and acts by permutation on the $N0$ columns of the table representing a_i ,
- or is any permutation of the symbols of a column of said table.

10 [0052] According to an eighth aspect, the present invention relates to a decoding device characterised in that it has a processing means adapted:

15 1/ to take into account:

- a predetermined integer $M1$, equal to or greater than 2,
- 10 a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:
 - 20 a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$ and has no multiple polynomial factors, and
 - a number of binary data equal to the product of any odd integer number M and the integer $N0$, the smallest integer such that the polynomial $x^{N0}+1$ is divisible by each of the polynomials $g_i(x)$;

25 2/ to perform an operation of parallel turbodecoding of K sequences of symbols using the divisor polynomials $g_{ij}(x)$.
3/ to effect a permutation operation producing so-called "permuted" sequences, a_{ij}^* ($i=1, \dots, K$; $j=1, \dots, M1$), each permuted sequence a_{ij}^* having a polynomial representation equal to $a_{ij}^*(x)=a_i(x^{e_{ij}})$ modulo (x^n+1) , where:

- 30 n is the product of the number M and the integer $N0$,
- e_{ij} is a relatively prime number with n
- c_{ij} is the quotient of $a_{ij}^*(x)$ by $g_{ij}(x)$,
- the polynomial $g_{ij}(x)$ is the generator polynomial of the smallest cyclic code of length $N0$ containing the polynomial $g_i(x^{e_{ij}})$ modulo $(x^{N0}+1)$,

35 at least one permuted sequence a_{ij}^* being different from the corresponding sequence a_i .

[0053] The invention also relates to:

- 40 an information storage means which can be read by a computer or a microprocessor storing instructions of a computer program, characterised in that it enables the method of the invention as briefly disclosed above to be implemented, and
- an information storage means which is removable, partially or totally, and which can be read by a computer or a microprocessor storing instructions of a computer program, characterised in that it enables the method of the invention as briefly disclosed above to be implemented. The invention also relates to:
 - 45 a device for processing signals representing speech, which includes a device as briefly disclosed above,
 - a data transmission device having a transmitter adapted to implement a packet transmission protocol, which includes a device as briefly disclosed above,
 - a data transmission device having a transmitter adapted to implement the ATM (Asynchronous Transfer Mode) packet transmission protocol, which has a device as briefly disclosed above.
 - 50 a data transmission device having a transmitter adapted to implement the packet transmission protocol, on a network of the ETHERNET (registered trade mark) type,
 - a network station, which has a device as briefly disclosed above,
 - a data transmission device having a transmitter transmitting on a non-cable channel, which has a device as briefly disclosed above, and
 - 55 a device for processing sequences of signals representing at most one thousand binary data, which has a device as briefly disclosed above.

[0054] As these coding and decoding devices, these coding and decoding methods and these signal processing, data transmission and sequence processing devices and this network have the same particular characteristics and the same

advantages as the coding method as briefly disclosed above, these particular characteristics and these advantages will not be repeated here.

[0055] The invention will be understood more clearly from a reading of the description which follows, made with regard to the accompanying drawings, in which:

- Figure 1 depicts schematically an electronic device incorporating a coder according to a first embodiment of the present invention;
- Figure 2 depicts schematically an operating flow diagram of a coder according to the first embodiment of the present invention, as illustrated in Figure 1;
- 10 - Figure 3 depicts schematically a flow diagram describing the steps of determination of an interlacer used in the device illustrated in Figure 1;
- Figure 4 depicts schematically a coder according to the second embodiment of the present invention;
- Figure 5 depicts schematically the general form of interlacers acting on several sequences of symbols to be coded;
- Figure 6 depicts a performance curve of particular examples of methods and devices according to the second embodiment of the present invention;
- 15 - Figure 7 depicts schematically an electronic device incorporating a coder according to a second embodiment of the present invention;
- Figure 8 depicts schematically an operating flow diagram of a coder according to the second embodiment of the present invention, as illustrated in Figure 7; and
- 20 - Figure 9 depicts schematically a decoding device to which the present invention relates.

[0056] In the following description, the first control sequence will always be obtained from non-interlaced information sequences, although the scope of the invention extends also to the general case.

[0057] The description of embodiments of the invention is, hereinafter, divided into two parts, respectively dedicated 25 to the case in which a single sequence of symbols is coded and to the case in which two sequences of symbols are simultaneously coded.

I - FIRST EMBODIMENT

30 [0058] In the description which follows, the term "data" will be given both to symbols representing information and to additional or redundant symbols.

[0059] Before beginning the description of a particular embodiment, the mathematical bases of its implementation are given below.

[0060] In the invention, $g(x)$, $h_1(x)$ and $h_2(x)$ being predetermined, it is stated that it is wished that the sequences b and c , defined respectively by the divisions $b(x) = a(x).h_1(x)/g(x)$ and $c(x) = a^*(x).h_2(x)/g(x)$, should have no remainder.

[0061] To this end, $g(x) = 1 + \sum_{i=1 \text{ to } m-1} g_i x^i + x^m$ being a polynomial of predetermined degree m , the smallest number $N0$ is sought such that $g(x)$ divides the polynomial $x^{N0} - 1$. It is known that this number exists. For example $g(x) = 1 + x + x^3$, $N0 = 7$.

[0062] Then, choosing any number M , a length of sequence a equal to $M.N0$ is chosen, which amounts to determining the length (that is to say the number of binary data) of the sequence u incorporated in the sequence a as being equal to $M.N0$ minus the degree of $g(x)$.

[0063] Thus, in order to form the sequence a , there is juxtaposed with the sequence u formed by k binary data u_i to be transmitted, a number of additional binary data equal to the degree of the polynomial $g(x)$, the added data guaranteeing the absence of a remainder in the division of $a(x)$ by $g(x)$.

[0064] It will be recalled that the division effected here is made, modulo 2, on the coefficients of the ascending powers of $a(x)$.

[0065] By way of example, if

50 the sequence u is the sequence (1, 0, 0, 1, 0, 0), and
the sequence g is the sequence (1, 1, 0, 1), the division is written:

5	1 0 0 1 0 0	1 1 0 1
	1 1 0 1	1 1 1 1 0 1
	1 1 0 1	
10	1 1 0 1	
	1 1 0 1	
	0 0 0 0	
15	1 1 0 1	
	0 0 0 0 0 0 0 1	

which is also written: $(1, 0, 0, 1, 0, 0, 0, 0, 0) = (1, 1, 0, 1) \times (1, 1, 1, 1, 0, 1) + (0, 0, 0, 0, 0, 0, 0, 1)$,
 20 that is to say also $(1, 0, 0, 1, 0, 0, 0, 0, 1) = (1, 1, 0, 1) \times (1, 1, 1, 1, 0, 1)$, adding, term by term, the remainder sequence $(0, 0, 0, 0, 0, 0, 0, 1)$ to the sequence u first of all supplemented by m "0"s.

25 [0066] Thus, by substituting, for the sequence $u = (1, 0, 0, 1, 0, 0, 0, 0)$, the sequence $a = (1, 0, 0, 1, 0, 0, 0, 1)$, formed by this addition, and the first binary data of which are all the binary data of the sequence u , the divisibility of the polynomial $a(x)$ by the polynomial $g(x)$ associated with the sequence $u = (1, 1, 0, 1)$ and, consequently, of $a(x) h_1(x)$ by $g(x)$, is guaranteed, whatever the sequence h_1 associated with the polynomial $h_1(x)$, which supplies the definition of the sequence b by $b(x) = a(x) h_1(x)/g(x)$.

30 [0067] In order to determine the sequence $a^*(x)$, which has, after permutation, the same binary data as the sequence a , but in a different order, an interlacer is chosen, a representation of which can be given as follows: the binary data of the sequence a being arranged in a table of N_0 columns and M rows, there is performed on these data at least one permutation in a set of permutations including, on the one hand, the automorphisms of the binary cyclic code of length N_0 and with the generator polynomial $g(x)$, permuting with each other at least two of the N_0 columns of the table and, on the other hand, the permutations operating solely on data in one and the same column and permuting with each other at least two of the said data items, and only one or more permutations of this set.

35 [0068] This is because the inventors have discovered that only the permutations which can be thus represented guarantee that, for any polynomial $a(x)$ whose division by $g(x)$ has no remainder, the permuted polynomial $a(x)$ has a division by $g(x)$ which has no remainder.

[0069] In such a succession, there can, for example where $N_0 = 7$ and $g(x) = 1 + x + x^3$, be found successively:

40 - a permutation of the binary data of the first column,
 - a permutation of the binary data of the third column,
 - the replacement of the second column by the fourth, the replacement of the fourth column by the second, the replacement of the fifth column by the sixth and the replacement of the sixth column by the fifth.

45 [0070] With regard to the automorphism, giving the name Cg to the binary cyclic code of length N_0 and with the generator polynomial $g(x)$, that is to say all the multiples of $g(x)$, modulo $x^{N_0}-1$, the permutations of the coordinates of this code which transform any word of this code into another word of this code are considered. The set of permutations of coordinates which have this property has a group structure and is called the Cg automorphism group.

50 [0071] For more details, the reader can refer to the work by Mrs F.J. MACWILLIAMS and Mr N. J. A. SLOANE, "The theory of error-correcting codes" published by North-Holland in 1977.

[0072] Amongst all these permutations, the inventors have selected the following permutations, which have the advantage of constituting only a small family, all the members of which can be tested in order to choose the most effective permutation.

55 [0073] As mentioned above, M is chosen so as to be odd and $g(x)$ such that the corresponding number N_0 is also odd. By writing the successive powers of 2 modulo $M \cdot N_0$, there is obtained what is called the cycle of 2, modulo $M \cdot N_0$. In this cycle, by choosing any term e , the following permutation is effected:

the polynomial $a(x)$ giving, after permutation, the polynomial $a^*(x)$, the latter is defined by $a^*(x) = a(x^e)$, thus, if $a = (a_0, a_1, a_2, \dots, a_{M \cdot N_0-1})$, the first binary data item of a^* is a_0 , the second a_f , the third a_{2f} , ..., f being the inverse

of e , modulo $M.N0$, and the multiples of f themselves being calculated modulo $M.N0$.

[0074] For example, by repeating $g(x) = 1 + x + x^3$, and therefore $N0 = 7$, and choosing $M = 5$, this gives $M.N0 = 35$. The cycle of 2 is then written:

[1, 2, 4, 8, 16, 32, 29, 23, 11, 22, 9, 18].

[0075] Taking, for example, $e = 2^8 = 11$, f will be equal to 16 and the sequence a' begins with the binary data: a_0 , a_{16} , a_{32} , a_{13} , a_{29} , a_{10} etc ...

[0076] These permutations which are described above and which can be represented by $a^*(x) = a(x^e)$ where e is in the cycle of 2 modulo $M.N0$, $a(x^e)$ being taken modulo $x^{M.N0}-1$, form a small family, all the members of which can be tested in order to choose the most effective.

[0077] The selection logic is as follows: first of all $g(x)$ of degree m , not divisible by a square polynomial, is chosen. This choice fixes the value of $N0$ as being the smallest integer such that $g(x)$ divides $x^{N0}-1$. In addition, the fact that the polynomial $g(x)$ is not divisible by a square polynomial implies that $N0$ is an odd number. Then $h_1(x)$ and $h_2(x)$ are chosen of any degree but preferentially at most equal to the degree m of $g(x)$ since the maximum of the degrees of these three polynomials $g(x)$, $h_1(x)$ and $h_2(x)$ is a determining factor in the complexity of the decoder. An odd integer M is then chosen and the cycle of 2 modulo $M.N0$ is calculated. An element e in this cycle of 2 is then chosen in order to specify $a^*(x) = a(x^e)$ modulo $x^{M.N0}-1$ from $a(x)$, and various testing operations are performed on the turbocode associated with the interlacer thus defined.

[0078] Let us take for example $g(x) = 1 + x + x^3$. this imposes $N0 = 7$. Let also $h_1(x) = 1 + x + x^2 + x^3$. $h_2(x) = 1 + x^2 + x^3$ and $M = 21$ be chosen, this leads to $M.N0=147$ and makes it possible to calculate the cycle of 2 modulo 147 as being {1, 2, 4, 8, 16, 32, 64, 128, 109, 71, 142, 137, 127, 107, 67, 134, 121, 95, 43, 86, 25, 50, 100, 53, 106, 65, 130, 113, 79, 11, 22, 44, 88, 29, 58, 116, 85, 23, 46, 92, 37, 74}.

[0079] By testing successively the polynomials $a(x)$ divisible by $g(x)$ of weight equal to 2, 3, 4 and 5, it is concluded

[0079] that the choice $e = 25$ is "promising" since the $a(x)$ polynomials of weight 2 then correspond to a coded sequence $v = (a, b, c)$ of weight ≥ 26 , the $a(x)$ polynomials of weight 3 corresponding then to a coded sequence $v = (a, b, c)$ of weight ≥ 26 , the weight ≥ 24 , the $a(x)$ polynomials of weight 4 then corresponding to a coded sequence $v = (a, b, c)$ of weight ≥ 30 etc.

[0080] $a(x)$ polynomials of weight 5 then corresponding to a coded sequence $v = (a, b, c)$ of weight ≥ 30 etc.

[0080] This seems to indicate a minimum distance equal to 24, which is the best value that can be obtained in accordance with the method disclosed above for $N0 = 7$ and $M = 21$ with $g(x)$, $h_1(x)$ and $h_2(x)$ as indicated above.

[0081] Another possible choice is $g(x) = 1 + x + x^4$, which imposes $N0 = 15$. Let also $h_1(x) = 1 + x + x^2 + x^4$, $h_2(x) = 1 + x^3 + x^4$ and $M = 27$ be chosen. This leads to $M.N0 = 405$ and makes it possible to calculate the cycle of 2 modulo 405 as being {1, 2, 4, 8, 16, ..., 304, 203}. It comprises 108 numbers.

[0082] Working by successive elimination, it is concluded that the choices $e = 151$, $e = 362$ and $e = 233$ are particularly promising.

[0083] In particular, for $e = 151$, the inventors have tested the polynomials $a(x)$ divisible by $g(x)$ and of weight equal successively to 2, 3, 4, 5, 6 and 7, and such that if this weight is greater than or equal to 5, then the weight of $a(x)$,

[0083] denoted $W(a(x))$, is equal to the weight of $a(x)$ modulo $x^{15}+1$.

[0084] When the weight of $a(x)$ is $W(a(x))$, the corresponding minimum weight of $W(v)$ is indicated in the table:

$W(a(x))$	$W(v) \geq$
2	54
3	42
4	44
5	48
6	54
7	54

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[0085] In the same way and under the same conditions, for $e = 362$, when the weight of $a(x)$ is $W(a(x))$, the minimum corresponding weight of $W(v)$ is indicated in the table:

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15

$W(a(x))$	$W(y) \geq$
2	54
3	42
4	42
5	50
6	56
7	54

[0086] According to the invention, the numbers e , non-congruent at 1, modulo $N0$, can be used in particular.

[0087] The description of a particular embodiment of the present invention will now be continued with regard to Figures 1 to 3.

[0088] Figure 1 illustrates schematically the constitution of a network station or computer coding station, in the form of a block diagram. This station has a keyboard 111, a screen 109, an external information source 110 and a radio transmitter 106, conjointly connected to an input/output port 103 of a processing card 101.

[0089] The processing card 101 has, connected together by an address and data bus 102:

25 - a central processing unit 100;
 - a random access memory RAM 104;
 - a read-only memory ROM 105;
 - the input/output port 103.

30 **[0090]** Each of the components illustrated in Figure 1 is well known to persons skilled in the art of microcomputers and transmission systems and, more generally, information processing systems. These common elements are therefore not described here. It will be observed, however, that:

35 - the information source 110 is, for example, an interface peripheral, a sensor, a demodulator, an external memory or another information processing system (not shown), and is preferentially adapted to supply sequences of signals representing speech, service messages or multimedia data, in the form of sequences of binary data,
 - the radio transmitter 106 is adapted to implement a packet transmission protocol on a non-cable channel, and to transmit these packets on such a channel.

[0091] It should also be noted that the word "register" used in the description designates, in each of the memories 104 and 105, both a memory area of low capacity (a few binary data) and a memory area of large capacity (making it possible to store an entire program).

[0092] The random access memory 104 stores data, variables and intermediate processing results, in memory registers bearing, in the description, the same names as the data whose values they store. The random access memory 104 has notably:

45 - a register "primary-data" in which there are stored, in the order of their arrival on the bus 102, the binary data coming from the information source 110, in the form of a sequence u , later supplemented to form a sequence a ,
 - a register " N^o _data" which stores an integer number corresponding to the number of binary data $n-m$ the register "binary_data",
 50 - a register "intermediate_remainder" in which there are stored successively the intermediate remainders of the division, a register used for constructing the sequence a from the sequence u ,
 - a register "final_remainder" in which there are stored the complementary binary data, in the form of a sequence,
 - a register "permuted_data" in which there are stored, in the order of their arrival on the bus 102, the permuted binary data, as described with regard to Figure 2, in the form of a sequence a^* , and
 55 - a register " a , b , c " which there are stored, in the order in which they are determined by the central unit 100, the binary data of the sequence currently being processed.

[0093] The read-only memory 105 is adapted to store, in registers which, for convenience, have the same names as

the data which they store:

- the operating program of the central processing unit 100, in a register "program".
- the sequence g , in a register "g".
- the degree m of $g(x)$, in a register "degree".
- the sequence h_1 , in a register "h₁".
- the sequence h_2 , in a register "h₂".
- the value of N_0 , in a register "N₀".
- the value of M , in a register "M", and
- the table defining the interlacer, in a register "interlacer".

[0094] The central processing unit 100 is adapted to implement the flow diagram described in Figure 2.

[0095] In Figure 2, which depicts the operation of a coder as illustrated in Figure 1, it can be seen that, after an initialisation operation 300, during which the registers of the random access memory 104 are initialised ($N^o_data = "0"$),

15 during an operation 301, the central unit 100 waits to receive, and then receives a binary data item to be transmitted,

positions it in the random access memory 104 in the register "primary_data" and increments the counter "N^o_data".

[0096] Next, during a test 302, the central unit 100 determines whether or not the integer number stored in the register "N^o_data" is equal to the product $M \cdot N_0$ from which the degree m of $g(x)$ being values stored in the read-only memory 105.

20 [0097] When the result of the test 302 is negative, the operation 301 is reiterated. When the result of the test 302 is positive, during an operation 303, the division of the polynomial $u(x)$ associated with the sequence of binary data stored in the register "primary_data" by the polynomial $g(x)$ is effected, up to the last term (of the highest degree) of $u(x)$, using, for this purpose, the register "intermediate_remainder", the remainder of this division is stored in memory in the register "final_remainder".

25 [0098] Next, during an operation 304, the binary data stored in the register "final_remainder" are juxtaposed at the end of the sequence u in order to form the sequence a . The binary data of the sequence a are stored in memory in the register "a, b, c".

[0099] Next, during an operation 305, the division effected during the operation 303 is continued, with the additional data added during the operation 304, and the sequence b is completed in the register "a, b, c".

30 [0100] Then, during an operation 306, the binary data of the sequence a are successively read from the register "a, b, c", in the order described by the table "interlacer" stored in the read-only memory 105. The data which result successively from this reading are stored in memory in the register "permuted_data" of the read-only memory 104.

[0101] Next, during an operation 307, the division of the polynomial $a^*(x)$ associated with the sequence of permuted binary data stored in the register "permuted_data" by the polynomial $g(x)$ is effected, using, for this purpose, the register "intermediate_remainder". The result of this division is stored in memory in the register "a, b, c", and corresponds to the binary data of the sequence c .

[0102] During an operation 308, the sequences b and c are determined by effecting the product of the polynomials associated with the sequences b and c stored in the register "a, b, c" of the random access memory 104, and respectively the polynomials $h_1(x)$ and $h_2(x)$.

40 [0103] It will be observed that, by virtue of the invention, memory elements are saved by effecting the division by $g(x)$ before the multiplication by $h_1(x)$ or $h_2(x)$.

[0104] During an operation 309, the sequences a , b , and c are sent, using for this purpose the sender 106. Next, the registers of the memory 104 are initialised again, in particular the counter "N^o_data" is reset to "0" and the operation 301 is reiterated.

45 [0105] It will be observed here that, as a variant, during the operation 309, the sequence a is sent as a whole, but only a sub-set, for example one data item out of two, of each of the sequences b and c is sent. This variant is known to persons skilled in the art as puncturing.

[0106] With regard to decoding, it will be observed that, by knowing the polynomials $g(x)$, $h_1(x)$, $h_2(x)$ and the interlacer which, from the sequence a , supply the permuted sequence a^* , a person skilled in the art knows, without any technical problem, how to produce the decoder adapted to decoding and the correction of any error affecting the triplet of sequences (a, b, c) by using the interlacer considered above and, optionally, the corresponding de-interlacer.

50 [0107] For this purpose, he can refer to:

- the article by Messrs. L.R. BAHL, J. COCKE, F. JELINEK and J. RAVIV entitled "Optimal decoding of linear codes for minimizing symbol error rate", published in the IEEE journal Transactions on Information Theory, in March 1974;
- the article by Messrs. J. HAGENAUER, E. OFFER and L. PARKE entitled "Iterative decoding of binary block and convolutional codes", published in IEEE journal Transactions on Information Theory, in March 1996;
- the article by Messrs. J. HAGENAUER and P. HOEHER entitled "A Viterbi algorithm with soft decision-outputs and

"its applications", published with the reports of the conference IEEE GLOBECOM, pages 1680-1686, in November 1989;

- the article by Messrs. J. HAGENAUER, P. ROBERTSON and L. PARKE entitled "Iterative (turbo)decoding of systematic convolutional codes with the MAP and SOVA algorithms", published by the journal Informationstechnische Gesellschaft (ITG) Fachbericht, pages 21 - 29, October 1994; and
- the article by Messrs. C. BERROU, S. EVANO and G. BATTAIL, entitled "Turbo-block-codes" and published with the reports of the seminar "Turbo Coding" organised by the Technology Institute of Lund (Sweden) (Department of Applied Electronics) in August 1996.

10 [0108] Figure 3 depicts the steps of an algorithm determining the value of e specifying the interlacer to use. These steps can be performed by a computer of a known type (not depicted), in which the registers "N0", "M", "interlacer", "d", "d_{max}", "e" and "j" are situated, in the random access memory.

15 [0109] During an operation 501, $g(x) = 1 + \sum_{i=1 \text{ to } m-1} g_i x^i + x^m$ being the predetermined polynomial of degree m which corresponds to the sequence g , the smallest strictly positive integer number $N0$ such that $g(x)$ divides the polynomial $x^{N0} - 1$ is sought. It is known that this number exists. For example, for $g(x) = 1 + x + x^3$, $N0 = 7$. To this end, the divisions of the polynomials $x^i - 1$ by $g(x)$ are effected successively, commencing with a value of i equal to the degree m of $g(x)$ and progressively incrementing i , with an incrementation step of 1, until the remainder of the division is nil, modulo 2. When the remainder is nil, the value of i is put in the register $N0$. It will be recalled that the division performed here is effected, modulo 2, on the coefficients of the ascending powers of $x^i - 1$.

20 [0110] Then, choosing an odd number M , so that the product $M.N0$ is greater than or equal to the number of binary data u , which must be transmitted in the same frame, added to the degree m of $g(x)$, during an operation 502, a length of sequence a equal to $M.N0$ is chosen, which amounts to determining the length (that is to say the number of binary data) of the sequence u incorporated in the sequence a as being equal to $M.N0$ minus the degree m of $g(x)$.

25 [0111] Then, during the operations 503 to 509, the central unit 100 determines whether the interlacer associated with e is to be taken into account, which means that there is no sequence a of low weight for which the sequence $v = (a, b, c)$ also has a low weight.

30 [0112] In the embodiment described and depicted, the determination of a^* will consist of replacing $a = (a_0, a_1, \dots)$ by $a^* = (a_0, a_1, a_2, \dots)$, where the multiples of f are calculated modulo $M.N0$. When f is equal to a power of 2 different from 1, modulo $M.N0$, this permutation is indeed of the type stated. It can in fact be represented by a permutation which 35 permutes binary data only within each column of the table, followed, when f is equal to a power of 2 different from 1, modulo $N0$, by a permutation of at least two of the columns with each other, this last permutation being an automorphism of the binary cyclic code of length $N0$ and with a generator polynomial $g(x)$. When f is equal to 1, modulo $N0$, this permutation relating to the columns is the "trivial" permutation or "identity" permutation, that is to say it maintains the position of the columns in the table.

35 [0113] To this end, in this particular embodiment of the present invention, during the operation 503, the central unit 100 determines the successive powers of 2 modulo $M.N0$, in order to obtain what is referred to as the cycle of 2, modulo $M.N0$, this cycle being completed as soon as one of the powers of 2 is equal to 1, modulo $M.N0$. The number of terms j of this cycle is stored in the register "j".

40 [0114] Then, during the operation 504, the intermediate values l and d_{max} stored in the registers "l" and "d_{max}" are initialised respectively to the value "1" and to the value "0".

45 [0115] Next, during an operation 505, the value of "l" is incremented by 1 and the l -th value of the cycle of 2, modulo $M.N0$, is taken.

50 [0116] Then, during an operation 506, if this value is not equal to 1 modulo $M.N0$, the weight of the sequence $v = (a, b, c)$ is determined for the sequences a of low weight, with the permutation defined by $a^*(x) = a(x^e)$ (thus, if $a = (a_0, a_1, a_2, \dots, a_{M.N0-1})$, the first binary data of a^* is a_0 , the second a_1 , the third a_2 , ..., as disclosed above, the index being calculated modulo $M.N0$).

55 [0117] To this end, since the distance between two sequences is the weight (that is to say the number of non-nil binary data) of the sequence constituted by the difference of the homologous binary data of these sequences, the process is limited to the analysis of the distance of the sequences with the nil sequence, the polynomials $a(x)$ are enumerated by ascending weight, the sum of the weights of the sequences in one and the same triplet (a, b, c) is measured and a search is made for the minimum weight for a given e , for the sequences a of low weight, and, once all these minimum weights have been determined for e in the cycle of 2, for the value of e which corresponds to the highest weight.

60 [0118] The distance is then stored in the register "d" of the random access memory 104. Next, if, during a test 507, the value stored in the register "d" is greater than the value stored in the register "d_{max}", then, during the operation 508, the value of the register "d_{max}" is modified in order to take the value d and the value of the l -th element of the cycle considered is stored in memory in the register "e".

65 [0119] Following the operation 508 or, when the result of the test 507 is negative, as long as the value of l is less than j , test 509, the operation 505 is reiterated.

[0120] The table "interlacer" is then formed as follows:

$a^*(x) = a(x)h_1(x)/g(x)$, thus if $\underline{a} = (a_0, a_1, a_2, \dots, a_{M \cdot N0-1})$, the first binary data item of \underline{a}^* is a_0 , the second a_1 , the third a_2 , ..., as disclosed above, the index being calculated modulo $M \cdot N0$.

[0121] According to a variant, not shown, the triplet $(\underline{a}, \underline{b}, \underline{c})$ is constructed as follows:

- $a(x)$ and $b(x) = a(x)h_1(x)/g(x)$ are defined as above.
- given a polynomial $g_2(x)$ chosen so that the smallest integer $N2$ such that $g_2(x)$ divides the polynomial $x^{N2} - 1$ is equal to the smallest integer $N0$ such that $g(x)$ divides the polynomial $x^{N0} - 1$, a permutation P is chosen which transforms any word of the binary cyclic code of length $N0$ and with a generator polynomial $g(x)$ into a word of the binary cyclic code of length $N2$ and with a generator polynomial $g_2(x)$. It will be noted that such a permutation exists only for the polynomials $g_2(x)$ generating cyclic codes equivalent to Cg . This verification is well known to persons skilled in the art and for this reference should be made to page 234 of the book by Mrs F.J. MACWILLIAMS and Mr N.J.A. SLOANE mentioned above;
- according to the invention, the permutation which, from the sequence \underline{a} , associated with the polynomial $a(x)$ divisible by $g(x)$, produces the sequence \underline{a}^{**} , associated with the polynomial $a^{**}(x)$, divisible by $g_2(x)$, is then produced by any permutation producing, from $a(x)$, a first sequence $a^*(x)$ divisible by $g(x)$ as explained above, followed by the permutation P which has just been introduced and which acts on the columns of the table with M rows and $N0$ columns containing first of all \underline{a} and next \underline{a}^* in order to permute these columns with each other and produce \underline{a}^{**} .

[0122] The scope of the invention is not limited to the embodiments described and depicted but quite the contrary extends to any modifications and improvements within the capability of persons skilled in the art.

[0123] In particular, passage at throughputs of a quarter or less, by adding one or more additional interlacers, is effected for each interlacer, by applying the principles set out above. In all these cases, puncturing can be used to raise the throughput of the code. It will be recalled that puncturing consists of transmitting only some of the check symbols.

[0124] In addition, devices which are the object of the present invention are advantageously produced by implementing, in order to effect the arithmetic calculations, polynomial multiplication, polynomial division, the function of interlacing and the functions of elementary decoding, dedicated circuits not including a processor (such a processor can nevertheless be used for controlling the operation of these devices). The use of such dedicated circuits makes it possible in fact to reach higher information flow rates.

[0125] It should be noted that, in the first embodiment, the throughput is, without puncturing, close to one third since, for a sequence of $n-m$ symbols to be coded, there are two sequences of n check symbols.

II - SECOND EMBODIMENT

[0126] In the second embodiment of the present invention, throughputs greater than $1/3$ are considered, obtained without puncturing: for two sequences of $n-m$ symbols to be coded, two sequences of n check symbols are for example supplied, that is to say a throughput close to one half.

[0127] Before beginning the description of the second embodiment, the mathematical bases of its implementation are given below.

[0128] In order to introduce the first embodiment, a class of algebraic interlacers to be used with turbocoders with a throughput close to one third is presented. The main advantage of these interlacers is to preserve the divisibility of the information polynomials by a given polynomial $g(x)$ which partially characterises the coder. As a result the probability of error per coded information bit is better independent of the position of the bits in the information sequence. As another advantage, the algebraic description of these interlacers makes their enumeration and individual evaluation possible. In addition, it is hoped that the performance of this small set of interlacers is representative of the performance of all the interlacers.

[0129] However, in many circumstances, for example in the context of wireless transmissions, a better throughput is necessary.

[0130] The second embodiment is concerned particularly with throughputs greater than or close to one half, without the use of puncturing methods.

IIa - High-throughput turbocodes with interlacers of the "x to x^e " type.

[0131] The following systematic convolutional coder $K \times (K+2)$ will be considered:

$$G = \begin{matrix} 1 & 0 & \dots & 0 & h_1/g & f_1/g \\ 0 & 1 & \dots & 0 & h_2/g & f_2/g \\ \dots & \dots & \dots & \dots & \dots & \dots \\ 0 & 0 & \dots & 1 & h_K/g & f_K/g \end{matrix} \quad (1)$$

10 in which h_i, f_i and g are polynomials with binary coefficients of indeterminate x representing the delay operator.
 [0132] In a conventional fashion, the transmitted information is represented by a K -tuple $\underline{a} = (a_1, \dots, a_K)$ of polynomials $a_i = \sum_{j=0 \text{ to } n-1} a_{ij} x^j$, with binary coefficients a_{ij} and the information is coded in $\underline{v} = \underline{a}G$, which is a $(K+2)$ -tuple of sequences of indeterminate x :

$$15 \quad \underline{v} = [a_1, \dots, a_K, (\sum_{i=1 \text{ to } K} a_i h_i)/g, (\sum_{i=1 \text{ to } K} a_i f_i)/g]$$

[0133] It should be noted that "sequences" rather than "polynomials" is written here, since the sums are not necessarily multiples of g and, if they are not, division by g makes a sequence infinite and ultimately periodic.

20 [0134] In order to improve the performance of this type of coder, the last component $(\sum_{i=1 \text{ to } K} a_i f_i)/g$ of \underline{v} can be replaced by $(\sum_{i=1 \text{ to } K} a_i^* f_i)/g$ where a_i^* represents the sequence obtained from the sequence a_i by permutation of its coefficients. The transformation of each sequence a_i into the sequence a_i^* is referred to as "interlacing" (see for example the article by Messrs. C. BERROU and A. GLAVIEUX entitled "Near Optimum error-correcting coding and decoding of turbo-codes" published by IEEE Transactions on Communication, Volume COM-44, pages 1261 to 1271, in October 1996).

25 [0135] Figure 4 gives an illustration of a coder performing this operation. In this figure, it will be observed that, for K sequences of symbols at the input, the coder sends, at the output:

- these K sequences of identical symbols,
- a sequence of check symbols formed by effecting the sum of the products of the polynomials associated with the information sequences a_i and predetermined polynomials h_i and dividing this sum by a predetermined polynomial g (coder 401);
- a sequence of check symbols formed by first of all interlacing each information sequence a_i by an interlacer l_i (interlacers 402 to 405) in order to supply a sequence a_i^* , then effecting the sum of the products of the polynomials associated with the sequences a_i^* and predetermined polynomials f_i and dividing this sum by a predetermined polynomial g (coder 406).

30 [0136] It should be noted here that the set of interlacers l_i 402 to 406 illustrated in Figure 1 is already a restriction of the interlacer 201 illustrated in Figure 5 in which each sequence a_i^* can contain symbols of the sequence a_j with j different from i .

40 [0137] According to general characteristics of the present invention, in a representation in which the binary data of each sequence \underline{a}_i are classified in a table of $N0$ columns and M rows, each interlacer l_i has:

- at least one permutation in a set of permutations including, on the one hand, the automorphisms of the binary cyclic code of length $N0$ and with a generator polynomial $g(x)$, permuting with each other at least two of the $N0$ columns of the table and, on the other hand, the permutations working solely on the data of the same column and permuting with each other at least two of the said data, and
- no permutation outside said set.

50 [0138] According to particular characteristics of the present invention, there is applied, to coders with a throughput $K/(K+2)$, with K representing an arbitrary positive integer value, interlacings of the type " x to x^n " described with regard to the first embodiment which concerns the value $K = 1$.

[0139] A description will now be given below of the case $K \geq 2$ (second embodiment).

[0140] Let a polynomial $g(x) = 1 + g_1 x + g_2 x^2 + \dots + g_{m-1} x^{m-1} + x^m$.

[0141] Let $N0$ be the smallest integer such that $g(x)$ divides $x^{N0} + 1$.

55 [0142] Finally, let n be equal to an odd multiple of $N0$: $n = M \cdot N0$.

[0143] The polynomial $g(x)$ is then a divisor of the polynomial $x^n + 1$. For example, with $g(x) = 1 + x + x^4$, n can be chosen amongst the values 15, 45, 75, ..., 225, ..., 405, ... Other details concerning these divisibility properties can be found in the work by W.W. PETERSON and E.J. WELDON entitled "Error-correcting codes" published by MIT Press,

Cambridge, Massachusetts, 1972.

[0144] The information is represented by a sequence $\underline{u} = (u_1, \dots, u_K)$ in which each of the K components u_i is represented by polynomial $u_i(x)$ of formal degree $n-m-1$ with binary coefficients. To each polynomial $u_i(x)$, there is added a termination, $\sum_{j=n-m \text{ to } n-1} (u_i)_j x^j$, a termination of m bits to make the polynomial $a_i = u_i + \sum_{j=n-m \text{ to } n-1} (u_i)_j x^j$ divisible by $g(x)$.

5 [0145] The resulting K -tuple $\underline{a} = (a_1, \dots, a_K)$ is then coded in order to produce two check sequences.

[0146] The first is given by $\sum_{i=1 \text{ to } K} a_i h_i / g$ and it is a polynomial because the polynomial $g(x)$ divides the K polynomials

10 a_i . The second is given by $\sum_{i=1 \text{ to } K} a_i f_i / g$, the interlacing of $a_i(x)$ into $a_i^*(x)$ being given by:

$$a_i^*(x) = a_i(x^e) \text{ modulo } x^n + 1 \quad (2)$$

where e is equal to a power of 2 ($e=2^l$) taken modulo n . This type of "x to x^e " permutation was presented in the first part concerning $K=1$ and guarantees the divisibility of a_i^* by g when a_i is divisible by g .

[0147] A few examples will now be given with $K=2$.

[0148] A 2×4 turbocoder of the form described in (1) and specified by $g(x) = 1 + x + x^3$;

15 $h_1(x) = f_2(x) = 1 + x^2 + x^3$; $h_2(x) = f_1(x) = 1 + x + x^2 + x^3$ and $n = 147$ will be considered.

[0149] With this value of n , 147, there are 42 numbers e which are each the residue, modulo 147, of a power of 2.

20 For each of these values of e , the corresponding turbocode was simulated on an additive white gaussian noise channel (known to persons skilled in the art under the English acronym "AWGN" standing for "Additive White Gaussian Noise"), for different values of the ratio between the energy per bit E_b and the noise power per hertz (also referred to as the noise

25 spectral density), N .

[0150] The corresponding values of the curves of the error rates per bit ("BER") as a function of the signal/noise ratio, are depicted in Figure 6, for $n=147$, $K=2$ and for three different values of e : $e = 67 = 2^{14}$, $e = 32 = 2^5$ and $e = 71 = 2^9$. The first two values represent "good" values of e , amongst the 42 possible values, and the last value of e represents

30 few "less good" values: 1, 2, 4, 109, 142 and 50.

[0151] With the same $g(x)$, $h_i(x)$, $f_i(x)$, for $i = 1$ or 2, but with a higher value of n , the same simulations can be effected. The cases $n = 413$ and $n = 917$ have been selected because they offer a large number of values of different powers of 2, modulo n . For $n = 413$, there are effectively 174 such different values, and for $n = 917$, there are 390 such different values.

35 [0152] The inventors observed that no level stage on the error curve seems to appear with the implementation of the present invention for a value of the error probability per bit after decoding of around 10^{-5} , when the value of e is chosen judiciously. It should also be noted that the interlacing of the $a_i(x)$ polynomials in order to produce $a_i^*(x) = a_i(x^e)$ modulo $x^n + 1$ can be effected for each value of i , with a different value of e but always with the form of an l^{th} power of 2: $e = 2^l$. Preferentially, the same interlacers are used for all the values of i , which preserves the identity of the k -tuples of symbols.

IIb - Specification of the turbocoders with $K \geq 2$

[0153] The following 3×5 turbocoder will for example be considered:

$$40 \quad G = \begin{matrix} 1 & 0 & 0 & h_1/g & f_1/g \\ 0 & 1 & 0 & h_2/g & f_2/g \\ 0 & 0 & 1 & h_3/g & f_3/g \end{matrix}$$

45

where g is an irreducible polynomial with binary coefficients which is not divisible by a square polynomial. This matrix G codes a triplet of information $\underline{u} = (u_1, u_2, u_3)$ as:

$$50 \quad v = [a_1, a_2, a_3, (\sum a_i h_i)/g, (\sum a_i^* f_i)/g]$$

where a_i is obtained from u and a_i^* from a_i , as disclosed with regard to the first embodiment.

[0154] An element which influences the minimum distances of such a code is the minimum number of non-nil components of the 5-tuple v .

55 [0155] It is possible to guarantee that any 5-tuple $v = (v_1, \dots, v_5)$ of the turbocode contains at least three non-nil sequences v_i .

[0156] In order to demonstrate this, a_i^* is written explicitly as $a_i(x^e)$ (reduced modulo $x^n + 1$), and the inverse of e

modulo n has been represented by "d":

[0157] $ed = 1 \pmod{n}$, an equation in which " (n) " means "modulo n ".

[0158] It is then noted that the equation $\sum a_i(x^e) f_i(x) = 0 \pmod{(x^n+1)}$ is equivalent to the equation $\sum a_i(x) f_i(x^d) = 0 \pmod{(x^n+1)}$.

[0159] This results from the fact that e and d are relatively prime with n , so that, for each $b(x)$ of degree less than or equal to $n-1$, $b(x^e)$ and $b(x^d)$, taken modulo (x^n+1) are simply obtained by permutation of the coefficients of $b(x)$, and that, if the polynomial $a(x^e)$ modulo (x^n+1) is denoted $[a(x)]^{1/e}$, this gives:

$$[a(x)f_i(x)]^{n/e} = [a(x)]^{n/e} [f_i(x)]^{n/e} \pmod{(x^n+1)}.$$

[0160] It results from the theory of codes known as "MDS" (standing for "Maximum Distance Separable", that any non-nil v in the code generated by G will always contain at least three non-nil components, if the following two conditions are satisfied:

- none of the polynomials h_i and f_i is nil modulo $x^{N0} + 1$, where $N0$ is the smallest integer such that $g(x)$ divides $x^{N0} + 1$, $N0$ being odd since the polynomial $g(x)$ is not divisible by any polynomial square, and
- no matrix 2×2 of the form

$$h_i(x) \quad f_i(x^d)$$

$$h_j(x) \quad f_j(x^d)$$

with i different from j , has a determinant which is nil, modulo $x^{N0} + 1$.

[0161] A similar property is valid for any coder of a turbocode of dimension K and length $N1$, with a number of redundancies $M1 = N1 - K > 2$. In the latter case, the coder resembles:

$$G = \begin{matrix} 1 & 0 & \dots & 0 & h_{1,1}/g & h_{1,2}/g & \dots & h_{1,N1-K}/g \\ 0 & 1 & \dots & 0 & h_{2,1}/g & h_{2,2}/g & \dots & h_{2,N1-K}/g \\ \dots & \dots \\ 0 & 0 & \dots & 1 & h_{K,1}/g & h_{K,2}/g & \dots & h_{K,N1-K}/g \end{matrix}$$

and any information sequence $u = (u_1, \dots, u_K)$ is first of all coded as $\underline{a} = (a_1, \dots, a_K)$, and then as:

$$v = [a_1, \dots, a_K, (\sum a_i h_{i,1})/g, (\sum a_i (x^{e^2}) h_{i,2})/g, \dots, (\sum a_i (x^{e^{N0-K}}) h_{i,K})/g]$$

[0162] Let d_i be the inverse of e_i modulo n : $d_i e_i = 1 \pmod{n}$. Each non-nil v in the code generated by G always contains at least $N1-K+1$ non-nil components if, for each integer number r such that $1 \leq r \leq N1-K$, each sub-matrix $r \times r$ of G extracted from its last $N1-K$ columns and where $h_{i,j}(x)$ is replaced by $h_{i,j}(x^{d_j})$, has a non-nil determinant, modulo $x^{N0} + 1$.

[0163] It should be noted here that the decoding of the redundancy turbocodes $N1 - K > 2$ has already been considered. For example, the article by D. DIVSALAR and F. POLLARA entitled "Multiple Turbocodes for Deep Space Communications", TDA Progress Report 42-121, of 15 May 1995, can be consulted.

[0164] A method for selecting good candidates for obtaining a good turbocode of dimensions K and length $N1$ with interlaces of the type "x to x^e " will now be described.

[0165] The case where $N1-K = 2$ will be considered first of all.

[0166] An irreducible polynomial $g(x)$ on $GF(2)$, of degree $m \geq 2$ such that $N0 = 2^m - 1 \geq N1$, will be chosen, and $GF(2^m)$ will be taken as the set of polynomial residues modulo $g(x)$. n will also be chosen as an odd multiple of $N0$. Then a matrix Γ with 2 rows and $N1$ columns will then be constructed:

$$\Gamma = \begin{matrix} \alpha_1^r & \alpha_2^r & \dots & \alpha_{N1}^r \\ \alpha_1^s & \alpha_2^s & \dots & \alpha_{N1}^s \end{matrix}$$

5 where α_i , $i = 1, \dots, N1$, are different non-nil elements of $GF(2^m)$ and r and s integers which are different modulo $N0$. The choice $s = r + 1$ is for example always a good choice. This implies that everything under the matrix Γ is non-singular. Let $\Gamma(1,2)$ be the sub-matrix of the first two columns of Γ . $[\Gamma(1,2)]^{-1} \Gamma$ will be written in the following way:

$$10 \quad [\Gamma(1,2)]^{-1} \Gamma = \begin{matrix} 1 & 0 \\ 0 & 1 \end{matrix} \Lambda$$

15 where Λ is a matrix $2 \times K$ on $GF(2^m)$. For a chosen value of e power of 2 modulo n , any element in the second row of Λ will be replaced by its e^{th} power and the transposed matrix of this matrix will be denoted Δ . The elements of Δ will then be interpreted as polynomials of degree $m-1$ of indeterminate x , and will be divided by $g(x)$ or by any other divisor polynomial of $x^{N0} + 1$ and the resulting matrix will be called $P(x)$.

19 [0167] Finally, the matrix G of dimension $K \times (K + 2)$ will be defined by:

$$G = [I_K P(x)]$$

20 where I_K is the identity matrix of dimension K .
[0168] For each value of e , this coder G can be used as a turbocoder. By simulation, it is then possible to choose the best value of e .

25 [0169] The case $N1 - K > 2$ can be treated in a similar fashion. In this case, with $M1 = N1 - K$, a matrix Γ is constructed of type $M1 \times N1$:

$$\Gamma = \begin{matrix} \alpha_1^r & \alpha_2^r & \dots & \alpha_{N1}^r \\ \alpha_1^{r+1} & \alpha_2^{r+1} & \dots & \alpha_{N1}^{r+1} \\ \dots & \dots & \dots & \dots \\ \alpha_1^{r+M1-1} & \alpha_2^{r+M1-1} & \dots & \alpha_{N1}^{r+M1-1} \end{matrix}$$

30 [0170] With $\Gamma(1, M1)$ the sub-matrix of the first $M1$ columns of Γ , $[\Gamma(1, M1)]^{-1} \Gamma$ as $[I_{M1} \Lambda]$ is written or I_{M1} is the identity matrix of dimension $M1$ and Λ a sub-matrix on $GF(2^m)$ of dimension $M1 \times K$. For chosen values $e_t = 2^{t^{\text{th}}}$, for $t = 2, \dots, M1$, the elements of the t^{th} line of Λ are replaced by their e_t^{th} power.

35 [0171] The transposed matrix of this matrix is then denoted Δ , the elements of Δ are interpreted as polynomials of degree $m-1$ of indeterminate x , they are divided by $g(x)$ and the resulting matrix of dimensions $K \times (N - K)$ is termed $P(x)$.

40 [0172] The coders $G = [I_K P(x)]$ obtained for different values of $(M1-1)$ -tuple (e_2, \dots, e_{M1}) are then analysed by simulations and the best can be selected.

45 IIc - Description of an implementation of the second embodiment of the present invention.

[0173] The description of the second embodiment of the present invention will now be continued with regard to Figures 7 and 8, for $K = M1 = 2$.

50 [0174] Figure 7 illustrates schematically the constitution of a network station or computer coding station, in the form of a block diagram. This station includes a keyboard 711, a screen 709, an external information source 710 and a radio transmitter 706, conjointly connected to an input/output port 703 of a processing card 701.

[0175] The processing card 701 has, connected together by an address and data bus 702:

55 - a central processing unit 700;
 - a random access memory RAM 704;
 - a read only memory ROM 705; and
 - the input/output port 703.

[0176] Each of the elements illustrated in Figure 7 is well known to persons skilled in the art of microcomputers and transmission systems and, more generally, information processing systems. These common elements are therefore not described here. It should however be noted that:

5 - the information source 710 is, for example, an interface peripheral, a sensor, a demodulator, an external memory or another information processing system (not shown), and is preferentially adapted to supply sequences of signals representing speech, service messages or multimedia data, in the form of sequences of binary data,

- the radio transmitter 706 is adapted to implement a packet transmission protocol on a non-cable channel and to transmit these packets on such a channel.

10 [0177] It should also be noted that the word "register" used in the description designates, in each of the memories 704 and 705, both a memory area of low capacity (a few binary data) and a memory area of large capacity (enabling an entire program to be stored).

15 [0178] The random access memory 704 stores data, variables and intermediate processing results, in memory registers bearing, in the description, the same names as the data whose values they store. The random access memory 704 contains notably:

20 - a register "primary_data" in which there are stored, in the order of their arrival on the bus 702, the binary data coming from the information source 710, in the form of two sequences, u_1 and u_2 , next supplemented in order to form two sequences a_1 and a_2 ,

- a register "No_data", which stores an integer number corresponding to the number of binary data $n-m$ in the register "binary_data",

- a register "permuted_data" in which there are stored, in the order of their transmission on the bus 702, the permuted binary data, as described with regard to Figure 8, in the form of two sequences a_1^* and a_2^* ,

25 - a register "intermediate_remainder" in which there are stored successively the intermediate remainders of the divisions, a register used for constructing each sequence a_i from the corresponding sequence u_i ,

- a register "final_remainder" in which there are stored the complementary binary data, in the form of two sequences, and

- registers " a_1 , b_1 , c_1 " and " a_2 , b_2 , c_2 " in which there are stored, in the order of their determination by the central 30 unit 700, the binary data of the sequences.

[0179] The read only memory 705 is adapted to store, in registers which, for convenience, bear the same names as the data which they store:

35 - the operating program of the central processing unit 700, in a register "program",

- the sequence g , in a register "g",

- the degree m of $g(x)$, in a register "degree"

- the sequence $h = h_1 = f_2$, in the register "h",

- the sequence $\bar{f} = f_1 = h_2$, in the register "f",

40 - the value of $N0$, in a register "N0",

- the value of $N1$, in a register "N1",

- the value of $M1$, in a register "M1",

- the value of M , in a register "M",

- the table defining the interlacer acting on the sequence a_1 , in a register "interlacer1", and

45 - the table defining the interlacer acting on the sequence a_2 , in a register "interlacer2".

[0180] The interlacers considered here are respectively of type " x to x^{e1} " and " x to x^{e2} " described above.

[0181] The central processing unit 700 is adapted to implement the flow diagram described in Figure 8.

50 [0182] In Figure 8, which depicts the functioning of a coder as illustrated in Figure 7, it can be seen that, after an initialisation operation 800, during which the registers of the random access memory 704 are initialised ($No_data = 0$), during an operation 801, the central unit 700 waits until it receives, and then receives a binary data item to be transmitted, positions it in the random access memory 704, in the register "primary_data" and increments the counter "No_data".

55 [0183] It should be noted here that, in order to constitute the two sequences u_1 and u_2 , the central unit 700 first of all constitutes the sequence u_1 , and then the sequence u_2 , with the primary data coming from the information source 710.

[0184] Next, during a test 802, the central unit 700 determines whether or not the integer number stored in the register "No_data" is equal to the product $M \cdot N0$ from which the degree m of $g(x)$, is subtracted $M \cdot N0$ and the degree m of $g(x)$ being values stored in the random access memory 705.

[0185] When the result of the test 802 is negative, the operation 801 is reiterated. When the result of the test 802 is positive, during an operation 803, the divisions of the polynomials $u_1(x)$ and $u_2(x)$ respectively associated with the sequences of binary data u_1 and u_2 stored in the register "primary_data", by the polynomial $g(x)$, are effected, up to the last terms (of the highest degrees) of $u_1(x)$ and $u_2(x)$, using, for this purpose, the register "intermediate_remainder". The results of these divisions supply the first elements of the sequences $b_1 = u_1/g$ and $b_2 = u_2/g$.

[0186] Next, during an operation 804, the binary data stored in the register "final_remainder" are respectively juxtaposed with the ends of the sequences u_1 and u_2 in order to form the sequences a_1 and a_2 . The binary data of the sequences a_1 and a_2 are stored in memory in the registers " a_1, b_1, c_1 " and " a_2, b_2, c_2 ".

[0187] Next, during an operation 805, the divisions effected during the operation 803 are continued, with the additional data added during the operation 804, and the sequences b_1 and b_2 are completed in the register " a_1, b_1, c_1 " and " a_2, b_2, c_2 ".

[0188] Then, during an operation 806:

15 - the binary data of the sequence a_1 are respectively and successively read in the register " a_1, b_1, c_1 ", in the order described by the table "interlacer1" stored in the random access memory 705, and

- the binary data of the sequence a_2 are respectively and successively read in the register " a_2, b_2, c_2 ", in the order described by the table "interlacer2" stored in the random access memory 705.

20 [0189] The data which results successively from these readings are respectively stored in memory in the register "permuted_data" of the random access memory 704.

[0190] Next, during an operation 807, the divisions of the polynomials $a_1^*(x)$ and $a_2^*(x)$, respectively associated with the sequences of permuted binary data stored in the register "permuted_data", by the polynomial $g(x)$ are effected, using for this purpose the register "intermediate_remainder". The results of these divisions are stored in memory in the register " a_1, b_1, c_1 " and " a_2, b_2, c_2 ", and correspond to the binary data of the sequences c_1 and c_2 .

25 [0191] During an operation 808, two so-called "check" or "redundant" sequences are determined:

- the sequence b_s is determined by effecting the product of the polynomials associated with the sequences b_1 and b_2 stored in the registers " a_1, b_1, c_1 " and " a_2, b_2, c_2 " in the random access memory 704 and respectively the polynomials $h(x)$ and $f(x)$;

- the sequence c_s is determined by effecting the product of the polynomials associated with the sequences c_1 and c_2 stored in the registers " a_1, b_1, c_1 " and " a_2, b_2, c_2 " in the random access memory 704 and respectively the polynomials $f(x)$ and $h(x)$.

35 [0192] It should be noted that, by virtue of the invention, memory elements are saved by effecting the division by $g(x)$ before the multiplications by $h(x)$ or $f(x)$.

[0193] During an operation 809, the sequences a_1, a_2, b_s and c_s are transmitted, using for this purpose the transmitter 706. Next the registers of the memory 704 are once again initialised, in particular the counter No_data is reset to "0" and the operation 801 is reiterated.

40 [0194] It should be noted here that, as a variant, during the operation 809, the sequences a_1 and a_2 are sent as a whole, but only a subset, for example one data item out of two, of each of the sequences b_s and c_s is sent. This variant is known to persons skilled in the art as puncturing.

[0195] With regard to decoding, it should be noted that, knowing the polynomials $g(x)$, $h(x)$, $f(x)$ and the interlacers G_1 and G_2 which, from sequences a_1 and a_2 respectively supply the permuted sequences a_1^* and a_2^* , a person skilled in the art knows, without any technical problem, how to produce the decoder and adapted to the decoding and error correction affecting the quadruplet of sequences (a_1, a_2, b_s, c_s) using the interlacers considered above and, possibly, the corresponding deinterlacers.

[0196] In Figure 9, it can be seen that a decoding device adapted to decode the sequences sent by the decoding device illustrated in Figures 4 to 8, has, essentially:

50 - a decoder 901 corresponding to the coder 401, which receives the estimations of transmitted sequences v_1 to v_{K+1} as well as K extrinsic information sequences w''_1 to w''_K disclosed below, and supplies K estimation sequences a posteriori w_1 to w_K .

- K interlacers 902, identical to the interlacers 402 to 405 used in the coder, which receive respectively the sequences w_1 to w_K and interlace them respectively as w'_1 to w'_K .

55 - a second decoder 903, corresponding to the coder 406 receiving the sequences w'_1 to w'_K as well as the sequence v_{K+2} , and supplies on the one hand K a posteriori estimation sequences w''_1 to w''_K and on the other hand an estimated sequence a' , and

- K deinterlacers 904, the reverse of the interlacers 402 to 405, receiving the sequences w'_1 to w'_{-K} and supplying the sequences w''_1 to w''_{-K} .

[0197] The estimated sequence \underline{a}' is taken into account only following a predetermined number of iterations (see the article "Near Shannon limit error-correcting coding and decoding : turbocodes" cited above).

[0198] In accordance with the present invention, the interlacers and deinterlacers used for decoding each have the same characteristics as the interlacers used for coding and preferentially, or of the type " x to $x^{\otimes n}$ ". Preferentially, for coding as for decoding, for an identical value of j the exponents e_{ij} are equal. Also preferentially, for coding as for decoding, the value of the exponents e_{ij} are all powers of 2.

[0199] In addition, in initialising the decoders 901 and 903, account is taken of the fact that the coders 401 and 406 each have an initial state and a final nil state.

[0200] Concerning decoding, the reader can refer:

- to the article by Messrs L.R. BAHL, J. COCKE, F. JELINEK and J. RAVIV entitled "Optimal decoding of linear codes for minimizing symbol error rate", published in the journal IEEE Transactions on Information Theory, in March 1974
- to the article by Messrs J. HAGENAUER, E. OFFER and L. PAPKE entitled "Iterative decoding of binary block and convolutional codes" published in the journal IEEE Transactions on Information Theory, in March 1996 ;
- to the article by Messrs J. HAGENAUER and P. HOEHER entitled "A Viterbi algorithm with soft decision outputs and its applications", published with the reports of the conference IEEE GLOBECOM, pages 1680-1686, in November 1989 ;
- to the article Messrs J. HAGENAUER, P. ROBERTSON and L. PAPKE entitled "Iterative (turbo)decoding of systematic convolutional codes with the MAP and SOVA algorithms", published by the journal Informationstechnische Gesellschaft (ITG) Fachbericht, pages 21 - 29, October 1994 ; and
- to the article by Messrs C. BERROU, S. EVANO and G. BATTAIL, entitled "Turbo-block-codes" and published with the reports of the seminar "Turbo Coding" organised by the Institute of Technology of Lund (Sweden) (Department of Applied Electronics) in August 1996.

Claims

1. Coding method characterised in that:

1/ it takes into account:

- a predetermined integer $M1$, equal to or greater than 2,
- a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:
 - a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$, and
 - a number of binary data equal to the product of any integer number M and the integer $N0$, the smallest integer such that the polynomial $x^{N0}+1$ is divisible by each of the polynomials $g_i(x)$;

2/ it includes a first operation of producing a number $K \times M1$ of so-called "permuted" sequences a_{ij}^* , ($i=1, \dots, K$; $j=1, \dots, M1$), each sequence a_{ij}^*

- being obtained by a permutation of the corresponding sequence a_i , said permutation being, in a representation where the binary data of each sequence a_i are written, row by row, in a table with $N0$ columns and M rows, the resultant of any number of so-called elementary permutations which, each:
 - either has the property of transforming the cyclic code of length $N0$ and with a generator polynomial $g_i(x)$ into an equivalent cyclic code with a generator polynomial $g_{ij}(x)$ which can be equal to $g_i(x)$, and acts by permutation on the $N0$ columns of the table representing a_i ,
 - or is any permutation of the symbols of a column of said table; and
- having, in consequence, a polynomial representation $a_{ij}^*(x)$ which is equal to a polynomial product $c_{ij}(x)g_{ij}(x)$,
- at least one permuted sequence a_{ij}^* being different from the corresponding sequence a_i ,

3/ it includes a second operation of producing $M1$ redundant sequences whose polynomial representation is equal to $\sum f_{ij}(x) c_{ij}(x)$, for $j=1, \dots, M1$, each polynomial $f_{ij}(x)$ being a polynomial with a degree at most equal to the degree of the polynomial $g_{ij}(x)$ with the same indices i and j .

5 2. Decoding method characterised in that:

1/ it takes into account:

- a predetermined integer $M1$, equal to or greater than 2,
- a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:
 - a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$ and has no multiple polynomial factors, and
 - a number of binary data equal to the product of any odd integer number M and the integer $N0$, the smallest integer such that the polynomial $x^{N0}+1$ is divisible by each of the polynomials $g_i(x)$;

15 2/ it includes a first operation of producing a number $K \cdot M1$ of so-called "permuted" sequences a_{ij}^* , ($i=1, \dots, K$; $j=1, \dots, M1$), each sequence a_{ij}^* having a polynomial representation equal to $a_{ij}^*(x) = a_i(x^{e_{ij}}) \bmod (x^{N0}+1)$, where

- n is the product of the number M and the integer $N0$,
- e_{ij} is a relatively prime number with n
- c_{ij} is the quotient of $a_{ij}^*(x)$ by $g_{ij}(x)$,
- the polynomial $g_{ij}(x)$ is the generator polynomial of the smallest cyclic code of length $N0$ containing the polynomial $g_i(x^{e_{ij}})$ modulo $(x^{N0}+1)$,
- at least one permuted sequence a_{ij}^* being different from the corresponding sequence a_i ;

20 3/ it includes a second operation of producing $M1$ redundant sequences whose polynomial representation is equal to $\sum f_{ij}(x) c_{ij}(x)$, for $j=1, \dots, M1$, each polynomial $f_{ij}(x)$ being a predetermined polynomial with a degree at least equal to the degree of the polynomial $g_{ij}(x)$ with the same indices i and j .

25 3. Coding method according to Claim 2, characterised in that, during the first production operation, all the values of the exponents e_{ij} having the same value of the index j are identical.

30 4. Coding method according to either one of Claims 2 or 3, characterised in that, during the first production operation, all the values of the exponents e_{ij} are equal to a power of 2.

35 5. Coding method according to any one of Claims 1 to 4, characterised in that it includes an operation of transmitting on the one hand sequences a_i , and, on the other hand, a sub-set of data of the other sequences.

40 6. Coding device characterised in that it includes a processing means adapted to:

45 1/ take into account:

- a predetermined integer $M1$, equal to or greater than 2,
- a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:

50 55 5. a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$, and

- a number of binary data equal to the product of any integer number M and the integer $N0$, the smallest integer such that the polynomial $x^{N0}+1$ is divisible by each of the polynomials $g_i(x)$;

55 2/ produce of a number $K \cdot M1$ of so-called "permuted" sequences, a_{ij}^* , ($i=1, \dots, K$; $j=1, \dots, M1$), each sequence a_{ij}^*

- being obtained by a permutation of the corresponding sequence, said permutation being, in a representation where the binary data of each sequence a_i are written, row by row, in a table with $N0$ columns and M

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rows, the resultant of any number of so-called elementary permutations which, each:

- either has the property of transforming the cyclic code of length $N0$ and with a generator polynomial $g_i(x)$ into an equivalent cyclic code with a generator polynomial $g_{ij}(x)$ which can be equal to $g_i(x)$, and acts by permutation on the $N0$ columns of the table representing a_i ,
- or is any permutation of the symbols of a column of said table; and
- having, in consequence, a polynomial representation $a_{ij}^*(x)$ which is equal to a polynomial product $c_{ij}(x)g_{ij}(x)$,
- at least one permuted sequence a_{ij}^* being different from the corresponding sequence a_i .

3/ produce $M1$ redundant sequences whose polynomial representation is equal to $\sum f_{ij}(x) c_{ij}(x)$, for $j=1, \dots, M1$, each polynomial $f_{ij}(x)$ being a polynomial with a degree at least equal to the degree of the polynomial $g_{ij}(x)$ with the same indices i and j .

7. Coding device characterised in that it has a processing means adapted to:

1/ take into account:

- a predetermined integer $M1$, equal to or greater than 2,
- a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:
 - a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$ and has no multiple polynomial factors, and
 - a number of binary data equal to the product of any odd integer number M and the integer $N0$, the smallest integer such that the polynomial $x^{N0}+1$ is divisible by each of the polynomials $g_i(x)$;

2/ produce a number $K \cdot M1$ of so-called "permuted" sequences a_{ij}^* , ($i=1, \dots, K$; $j=1, \dots, M1$), each sequence a_{ij}^* having a polynomial representation equal to $a_{ij}^*(x) = a_i^*(x^{e_{ij}}) \bmod (x^n+1)$, where

- n is the product of the number M and the integer $N0$,
- e_{ij} is a relatively prime number with n
- c_{ij} is the quotient of $a_{ij}^*(x)$ by $g_{ij}(x)$,
- the polynomial $g_{ij}(x)$ is the generator polynomial of the smallest cyclic code of length $N0$ containing the polynomial $g_i(x^{e_{ij}}) \bmod (x^{N0}+1)$,
- at least one permuted sequence a_{ij}^* being different from the corresponding sequence a_i ;

3/ produce $M1$ redundant sequences whose polynomial representation is equal to $\sum f_{ij}(x) c_{ij}(x)$, for $j=1, \dots, M1$, each polynomial $f_{ij}(x)$ being a predetermined polynomial with a degree at least equal to the degree of the polynomial $g_{ij}(x)$ with the same indices i and j .

8. Coding device according to Claim 7, characterised in that the processing means is adapted to use exponents e_{ij} which, when they have the same value of the index j , are identical.

9. Coding device according to either one of Claims 7 or 8, characterised in that the processing means is adapted to use exponents e_{ij} which each have a value equal to a power of 2.

10. Coding device according to any one of Claims 6 to 9, characterised in that it has a transmission means adapted to transmit on the one hand the sequences a_i , and, on the other hand, a sub-set of the data of the other sequences.

11. Decoding method characterised in that:

1/ it takes into account:

- a predetermined integer $M1$, equal to or greater than 2,
- a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:

- a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$, and
- a number of binary data equal to the product of any integer number M and the integer $N0$, the smallest integer such that the polynomial $x^{N0}+1$ is divisible by each of the polynomials $g_i(x)$;

5 2/ it includes an operation of parallel turbodecoding of K sequences of symbols using the divisor polynomials $g_{ij}(x)$.

3/ it includes, for each a_i , $M1$ permutation operations, at least one of which is not identity, each permutation being, in a representation where the binary data of each sequence a_i are written, row by row, in a table with $N0$ columns and M rows, the resultant of any number of so-called elementary permutations which, each:

- either has the property of transforming the cyclic code of length $N0$ and with a generator polynomial $g_i(x)$ into an equivalent cyclic code with a generator polynomial $g_{ij}(x)$ which can be equal to $g_i(x)$, and acts by permutation on the $N0$ columns of the table representing a_i ,
- or is any permutation of the symbols of a column of said table.

15 12. Decoding method characterised in that:

1/ it takes into account:

- a predetermined integer $M1$, equal to or greater than 2,
- a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:
 - a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$ and which has no multiple polynomial factors, and
 - a number of binary data equal to the product of any odd integer number M and the integer $N0$, the smallest integer such that the polynomial $x^{N0}+1$ is divisible by each of the polynomials $g_i(x)$;

2/ it includes an operation of parallel turbodecoding of K sequences of symbols using the divisor polynomials $g_{ij}(x)$.

3/ the said parallel turbodecoding operation including a permutation operation producing so-called "permuted" sequences, a_{ij}^* , ($i=1, \dots, K$; $j=1, \dots, M1$), each permuted sequence a_{ij}^* having a polynomial representation equal to $a_{ij}^*(x) = a_i(x^{eij})$ modulo (x^n+1) , where:

- n is the product of the number M and the integer $N0$,
- e_{ij} is a relatively prime number with n
- c_{ij} is the quotient of $a_{ij}^*(x)$ by $g_{ij}(x)$,
- the polynomial $g_{ij}(x)$ is the generator polynomial of the smallest cyclic code of length $N0$ containing the polynomial $g_i(x^{eij})$ modulo $(x^{N0}+1)$,

40 at least one permuted sequence being different from the corresponding sequence a_i ,

13. Decoding method according to Claim 12, characterised in that, during the permutation operation, all the values of the exponents e_{ij} having the same value of the index j are identical.

45 14. Decoding method according to either one of Claims 12 or 13, characterised in that, during the permutation operation, all the values of the exponents e_{ij} are equal to a power of 2.

15. Decoding method according to any one of Claims 11 to 14, characterised in that it includes an operation of receiving on the one hand sequences a_i , and on the other hand a sub-set of the data of other sequences resulting from 50 a coding of the sequences a_i .

16. Permutation method in an interlacer characterised in that:

1/ it takes into account:

- a predetermined integer $M1$, equal to or greater than 2,
- a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:

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- a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$, and
- a number of binary data equal to the product of any integer number M and the integer $N0$, the smallest integer such that the polynomial $x^{N0} + 1$ is divisible by each of the polynomials $g_i(x)$;

5 2/ it includes a first operation of producing a number $K \cdot M1$ of so-called permuted" sequences a_{ij}^* , ($i=1, \dots, K$; $j=1, \dots, M1$), each sequence a_{ij}^*

- being obtained by a permutation of the corresponding sequence a_i , said permutation being, in a representation where the binary data of each sequence a_i are written, row by row, in a table with $N0$ columns and M rows, the resultant of any number of so-called elementary permutations which, each:

 - either has the property of transforming the cyclic code of length $N0$ and with a generator polynomial $g_i(x)$ into an equivalent cyclic code with a generator polynomial $g_{ij}(x)$ which can be equal to $g_i(x)$, and
 - acts by permutation on the $N0$ columns of the table representing a_i ,
 - or is any permutation of the symbols of a column of said table; and
 - having, in consequence, a polynomial representation $a_{ij}^*(x)$ which is equal to a polynomial product $c_{ij}(x)g_{ij}(x)$,
 - at least one permuted sequence a_{ij}^* being different from the corresponding sequence a_i .

10 17. Permutation method supplying, from a sequence \underline{a} of binary data representing a physical quantity, associated with a polynomial $a(x)$ divisible by a divisor polynomial $g(x)$ and whose coefficients of ascending order are the binary data of the sequence \underline{a} , a permuted sequence \underline{a}' associated with a polynomial $a^*(x)$ whose coefficients of ascending order are the binary data of the sequence \underline{a}' , the said polynomial $a^*(x)$ being intended to be divided by the polynomial $g(x)$, in order to form a sequence of binary data \underline{c} , and \underline{a} having a number of binary data equal to the product of any integer number M and the integer $N0$, $N0$ being the smallest integer such that $x^{N0} - 1$ is divisible by the polynomial $g(x)$.

15 characterised in that, in a representation in which the binary data of the sequence \underline{a} are arranged in a table of $N0$ columns and M rows, it includes:

20

- at least one permutation (306) in a set of permutations including, on the one hand, the automorphisms of the binary cyclic code of length $N0$ and with a generator polynomial $g(x)$, permuting with each other at least two of the $N0$ columns of the table and, on the other hand, the permutations operating solely on data of one and the same column and permuting with each other at least two of the said data items, and
- no permutation outside the said set.

25 18. Permutation method supplying, from a sequence \underline{a} of binary data representing a physical quantity, represented by a polynomial $a(x)$ divisible by a divisor polynomial $g(x)$, a permuted sequence \underline{a}' represented by a polynomial $a^*(x)$, data \underline{c} .

30 characterised in that, in a representation in which the binary data of the sequence \underline{a} are arranged in a table of $N0$ columns and M rows, it includes:

35

- at least one permutation (306) in a set of permutations including, on the one hand, the automorphisms of the binary cyclic code of length $N0$ and with a generator polynomial $g(x)$, permuting with each other at least two of the $N0$ columns of the table and, on the other hand, the permutations operating solely on data of one and the same column and permuting with each other at least two of the said data items; and
- no permutation outside the said set.

40 19. Permutation method supplying, from a sequence \underline{a} of binary data representing a physical quantity, represented by a polynomial $a(x)$ divisible by a divisor polynomial $g(x)$, a permuted sequence \underline{a}' represented by a polynomial $a^*(x)$, data \underline{c} .

45 characterised in that, in a representation in which the binary data of the sequence \underline{a} are arranged in a table of $N0$ columns and M rows, it includes:

50

- at least one permutation (306) in a set of permutations including, on the one hand, the automorphisms of the binary cyclic code of length $N0$ and with a generator polynomial $g(x)$, permuting with each other at least two of the $N0$ columns of the table and, on the other hand, the permutations operating solely on data of one and the same column and permuting with each other at least two of the said data items; and
- no permutation outside the said set.

55 20. Permutation method supplying, from a sequence \underline{a} of binary data representing a physical quantity, associated with a polynomial $a(x)$ divisible by a divisor polynomial $g(x)$ and whose coefficients of ascending order are the binary

5 data of the sequence \underline{a} , a permuted sequence \underline{a}'' associated with a polynomial $a''(x)$ whose coefficients of ascending order are the binary data of the sequence \underline{a}'' , the said polynomial $a''(x)$ being intended to be divided by a divisor polynomial $g_2(x)$, in order to form a sequence of binary data \underline{c} and \underline{a} having a number of binary data equal to the product of any integer number M and the integer N_0 , N_0 being the smallest integer such that $x^{N_0} - 1$ is divisible by the polynomial $g(x)$.

10 characterised in that, in a representation where the binary data of the sequence \underline{a} are arranged in a table of N_0 columns and M rows, it includes:

- 15 - at least one permutation (306) in a set of permutations including, on the one hand, the automorphisms of the binary cyclic code of length N_0 and with a generator polynomial $g(x)$, permuting with each other at least two of the N_0 columns of the table, and, on the other hand, the permutations operating solely on data of one and the same column and permuting with each other at least two of the said data items, thus producing a sequence $a'(x)$, and
- 20 - a permutation of the columns of the said table which transforms the polynomial $a'(x)$ into the polynomial $a''(x)$ divisible by the polynomial $g_2(x)$.

25 21. Permutation method according to any one of Claims 17 to 20, characterised in that it includes at least one permutation operation (306) operating only on the binary data of one of the said columns.

30 22. Permutation method according to any one of Claims 17 to 21, characterised in that the said permutation operation (306) is effected as follows:

$$a''(x) = a(x^e), \text{ modulo } x^{M \cdot N_0} - 1,$$

35 25 where e is an integer value equal to a power of 2, modulo $M \cdot N_0$ and M is an odd number.

40 23. Permutation method according to any one of Claims 17 to 22, characterised in that it includes an operation of determining, from the sequence of binary data \underline{a} , at least a second sequence permuted by implementing a method according to any one of Claims 17 to 22.

45 24. Permutation method according to any one of Claims 17 to 23, characterised in that it includes an operation (309) of transmitting on the one hand the sequence \underline{a} , and on the other hand a sub-set of the data of the other sequences.

50 25. Decoding device characterised in that it includes a processing means adapted:

1/ to take into account:

- 40 - a predetermined integer M_1 , equal to or greater than 2,
- a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:
 - a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$, and
 - a number of binary data equal to the product of any integer number M and the integer N_0 , the smallest integer such that the polynomial $x^{N_0} + 1$ is divisible by each of the polynomials $g_i(x)$;

55 2/ to perform an operation of parallel turbodecoding of K sequences of symbols using the divisor polynomials $g_{ij}(x)$.

3/ to perform, for each a_i , M_1 permutation operations, at least one of which is not identity, each permutation being, in a representation where the binary data of each sequence a_i are written, row by row, in a table with N_0 columns and M rows, the resultant of any number of so-called elementary permutations which, each:

- either has the property of transforming the cyclic code of length N_0 and with a generator polynomial $g_i(x)$ into an equivalent cyclic code with a generator polynomial $g_{ij}(x)$ which can be equal to $g_i(x)$, and acts by permutation on the N_0 columns of the table representing a_i ,
- or is any permutation of the symbols of a column of said table.

55 26. Decoding device characterised in that it has a processing means adapted:

1/ to take into account:

- a predetermined integer $M1$, equal to or greater than 2,
- a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:
 - a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$ and has no multiple polynomial factors, and
 - a number of binary data equal to the product of any odd integer number M and the integer $N0$, the smallest integer such that the polynomial $x^{N0}+1$ is divisible by each of the polynomials $g_i(x)$;

2/ to perform an operation of parallel turbodecoding of K sequences of symbols using the divisor polynomials $g_{ij}(x)$.

3/ to effect a permutation operation producing so-called "permuted" sequences, a_{ij}^* , ($i=1, \dots, K$; $j=1, \dots, M1$), each permuted sequence a_{ij}^* having a polynomial representation equal to $a_{ij}^*(x) = a_i(x^{e_{ij}})$ modulo (x^n+1) , where:

- n is the product of the number M and the integer $N0$,
- e_{ij} is a relatively prime number with n
- c_{ij} is the quotient of $a_{ij}^*(x)$ by $g_{ij}(x)$,
- the polynomial $g_{ij}(x)$ is the generator polynomial of the smallest cyclic code of length $N0$ containing the polynomial $g_i(x^{e_{ij}})$ modulo $(x^{N0}+1)$.

at least one permuted sequence a_{ij}^* being different from the corresponding sequence a_i .

25 27. Decoding device according to Claim 26, characterised in that the processing means is adapted to use values of the exponents e_{ij} which are identical, when said exponents have the same value of the index j .

28. Decoding device according to either one of Claims 26 or 27, characterised in that the processing means is adapted to use values of the exponents e_{ij} which are each equal to a power of 2.

30 29. Decoding device according to one of Claims 25 to 28, characterised in that it includes a reception means adapted to receive, on the one hand sequences a_i , and on the other hand a sub-set of the data of other sequences resulting from a coding of the sequences a_i .

35 30. Interlacer characterised in that it includes a processing means adapted to:

1/ take into account:

- a predetermined integer $M1$, equal to or greater than 2,
- a number K , greater than or equal to 1, of sequences a_i ($i=1, \dots, K$) of binary data representing a physical quantity, each sequence a_i having:
 - a polynomial representation $a_i(x)$ which is a multiple of a predetermined polynomial $g_i(x)$, and
 - a number of binary data equal to the product of any integer number M and the integer $N0$, the smallest integer such that the polynomial $x^{N0}+1$ is divisible by each of the polynomials $g_i(x)$;

2/ produce a number K^*M1 of so-called "permuted" sequences, a_{ij}^* , ($i=1, \dots, K$; $j=1, \dots, M1$), each sequence a_{ij}^*

- being obtained by a permutation of the corresponding sequence, said permutation being, in a representation where the binary data of each sequence a_i are written, row by row, in a table with $N0$ columns and M rows, the resultant of any number of so-called elementary permutations which, each:
 - either has the property of transforming the cyclic code of length $N0$ and with a generator polynomial $g_i(x)$ into an equivalent cyclic code with a generator polynomial $g_j(x)$ which can be equal to $g_i(x)$, and acts by permutation on the $N0$ columns of the table representing a_i ,
 - or is any permutation of the symbols of a column of said table; and
- having, in consequence, a polynomial representation $a_{ij}^*(x)$ which is equal to a polynomial product

$c_{ij}(x)g_{ij}(x)$,

- at least one permuted sequence a_{ij}' being different from the corresponding sequence a_{ij} .

31. Interlacer (101) adapted to supply, from a sequence a of binary data representing a physical quantity, associated with a polynomial $a(x)$ divisible by a divisor polynomial $g(x)$ and whose coefficients of ascending order are the binary data of the sequence a , a permuted sequence a' associated with a polynomial $a^*(x)$ whose coefficients of ascending order are the binary data of the sequence a^* , the said polynomial $a^*(x)$ being intended to be divided by the polynomial $g(x)$ in order to form a sequence of binary data c , and a having a number of binary data equal to the product of any integer number M by the integer $N0$, $N0$ being the smallest integer such that $x^{N0} - 1$ is divisible by the polynomial $g(x)$.

10 characterised in that, in a representation in which the binary data of the sequence a are arranged in a table of $N0$ columns and M rows, it is adapted to use:

15 - at least one permutation (306) in a set of permutations including, on the one hand, the automorphisms of the binary cyclic code of length $N0$ and with a generator polynomial $g(x)$, permuting with each other at least two of the $N0$ columns of the table and, on the other hand, the permutations operating solely on data of one and the same column and permuting with each other at least two of the said data items, and

20 - no permutation outside the said set.

25 32. Interlacer (101) adapted to supply, from a sequence a of binary data representing a physical quantity, represented by a polynomial $a(x)$ divisible by a divisor polynomial $g(x)$, a permuted sequence a' represented by a polynomial $a^*(x)$, the said polynomial $a^*(x)$ being intended to be divided by the polynomial $g(x)$ in order to form a sequence of binary data c .

30 characterised in that, in a representation in which the binary data of the sequence a are arranged in a table of $N0$ columns and M rows, it is adapted to use:

35 - at least one permutation (306) in a set of permutations including, on the one hand, the automorphisms of the binary cyclic code of length $N0$ and with a generator polynomial $g(x)$, permuting with each other at least two of the $N0$ columns of the table and, on the other hand, the permutations operating solely on data of one and the same column and permuting with each other at least two of the said data items, and

40 - no permutation outside the said set.

45 33. Interlacer (101) adapted to supply, from a sequence a of binary data representing a physical quantity, represented by a polynomial $a(x)$ divisible by a divisor polynomial $g(x)$, a permuted sequence a' represented by a polynomial $a^*(x)$, the said polynomial $a^*(x)$ being intended to be divided by the polynomial $g(x)$ in order to form a sequence of binary data c , and a having a number of binary data equal to the product of any integer number M by the integer $N0$, $N0$ being the smallest integer such that $x^{N0} - 1$ is divisible by the polynomial $g(x)$.

50 34. Interlacer (101) adapted to supply, from a sequence a of binary data representing a physical quantity, associated with a polynomial $a(x)$ divisible by a divisor polynomial $g(x)$ and whose coefficients of ascending order are the binary data of the sequence a , a permuted sequence a'' associated with a polynomial $a^{**}(x)$ whose coefficients of ascending order are the binary data of the sequence a'' , the said polynomial $a^{**}(x)$ being intended to be divided by a divisor polynomial $g_2(x)$ in order to form a sequence of binary data c , and a having a number of binary data equal to the product of any integer number M and the integer $N0$, $N0$ being the smallest integer such that $x^{N0} - 1$ is divisible by the polynomial $g(x)$.

55 characterised in that, in a representation in which the binary data of the sequence a are arranged in a table of $N0$ columns and M rows, it is adapted to implement:

- at least one permutation (306) in a set of permutations including, on the one hand, the automorphisms of the binary cyclic code of length $N0$ and with a generator polynomial $g(x)$, permuting with each other at least two of the $N0$ columns of the table and, on the other hand, the permutations operating solely on data of one and the same column and permuting with each other at least two of the said data items, thus producing a sequence $a^*(x)$, and
- a permutation of the columns of the said table which transforms the polynomial $a^*(x)$ into the polynomial $a^{**}(x)$ divisible by the polynomial $g_2(x)$.

35. Interlacer according to any one of Claims 30 to 34, characterised in that the interlacer is adapted so that the said permutation (306) includes at least one permutation operation operating only on the binary data of one of the said columns.

5 36. Interlacer according to any one of Claims 30 to 35, characterised in that the interlacer (101) is adapted to perform the said permutation as follows:

$$a^*(x) = a(x^e), \text{ modulo } x^{M.N_0-1}$$

10 where e is an integer value equal to a power of 2, modulo $M.N0$ and M is an odd number.

15 37. Interlacer according to any one of Claims 30 to 36, characterised in that it also includes at least a second interlacer according to either one of Claims 10 or 11, each new interlacer being adapted to supply, from the sequence of binary data a , a new permuted sequence.

20 38. Interlacer (101) according to any one of Claims 30 to 37, characterised in that it includes a transmission means (106) adapted to transmit on the one hand the sequence a and on the other hand a sub-set of the data of the other sequences.

25 39. Device for processing signals representing speech, characterised in that it includes a coding device according to one of Claims 6 to 10 or a decoding device according to one of Claims 25 to 29 or an interlacer according to any one of claims 30 to 38.

30 40. Data transmission device having a transmitter adapted to implement a packet transmission protocol, characterised in that it includes a coding device according to any one of Claims 6 to 10 or a decoding device according to any one of Claims 25 to 29 or a device for processing signals representing speech according to Claim 39 or an interlacer according to any one of claims 30 to 38.

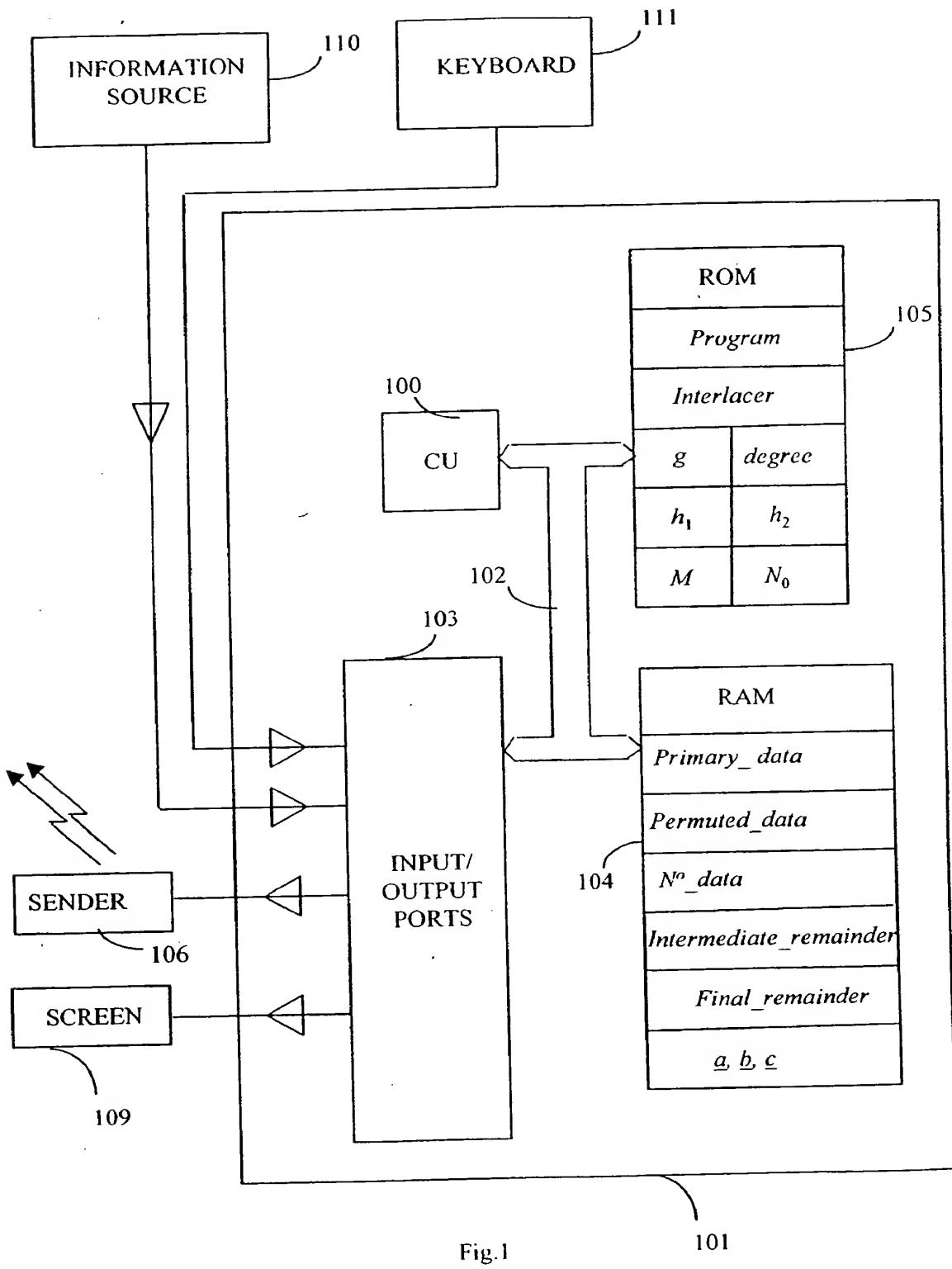
35 41. Data transmission device according to Claim 40, characterised in that said protocol is the asynchronous transfer mode protocol ATM (acronym of the English words "Asynchronous Transfer Mode").

40 42. Data transmission device according to Claim 40, characterised in that said protocol is a protocol of the ETHERNET type.

45 43. Data transmission device having a transmitter transmitting over a non-cable channel, characterised in that it includes a coding device according to any one of Claims 6 to 10 or a decoding device according to any one of Claims 25 to 29 or an interlacer according to any one of claims 30 to 38.

50 44. Device for processing sequences of signals representing at most one thousand binary data, characterised in that it includes a coding device according to any one of Claims 6 to 10 or a decoding device according to any one of Claims 25 to 29 or an interlacer according to any one of claims 30 to 38.

55 45. Network station, characterised in that it has a coding device according to any one of Claims 6 to 10 or a decoding device according to any one of Claims 25 to 29 or an interlacer according to any one of claims 30 to 38.



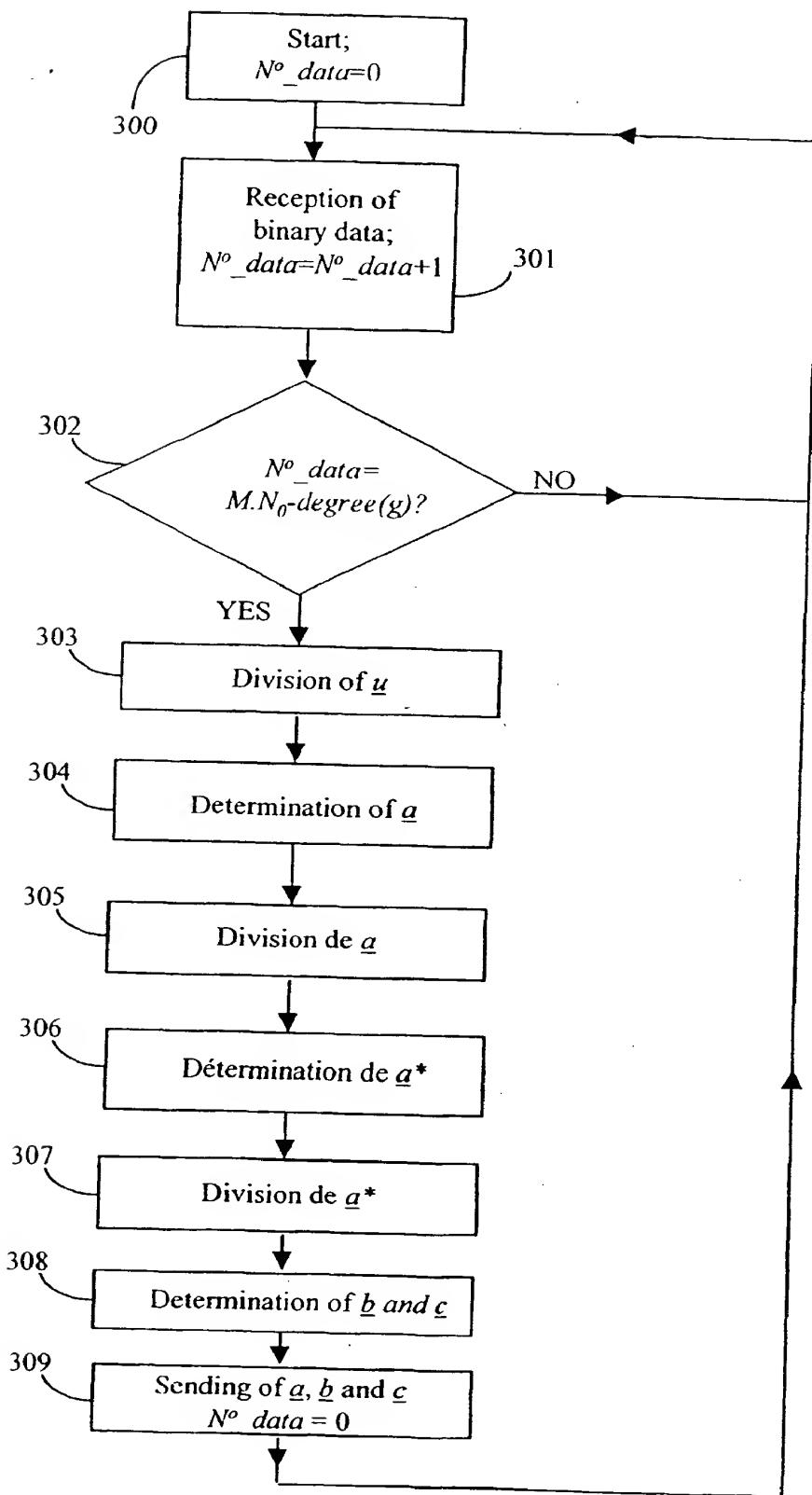


Fig.2

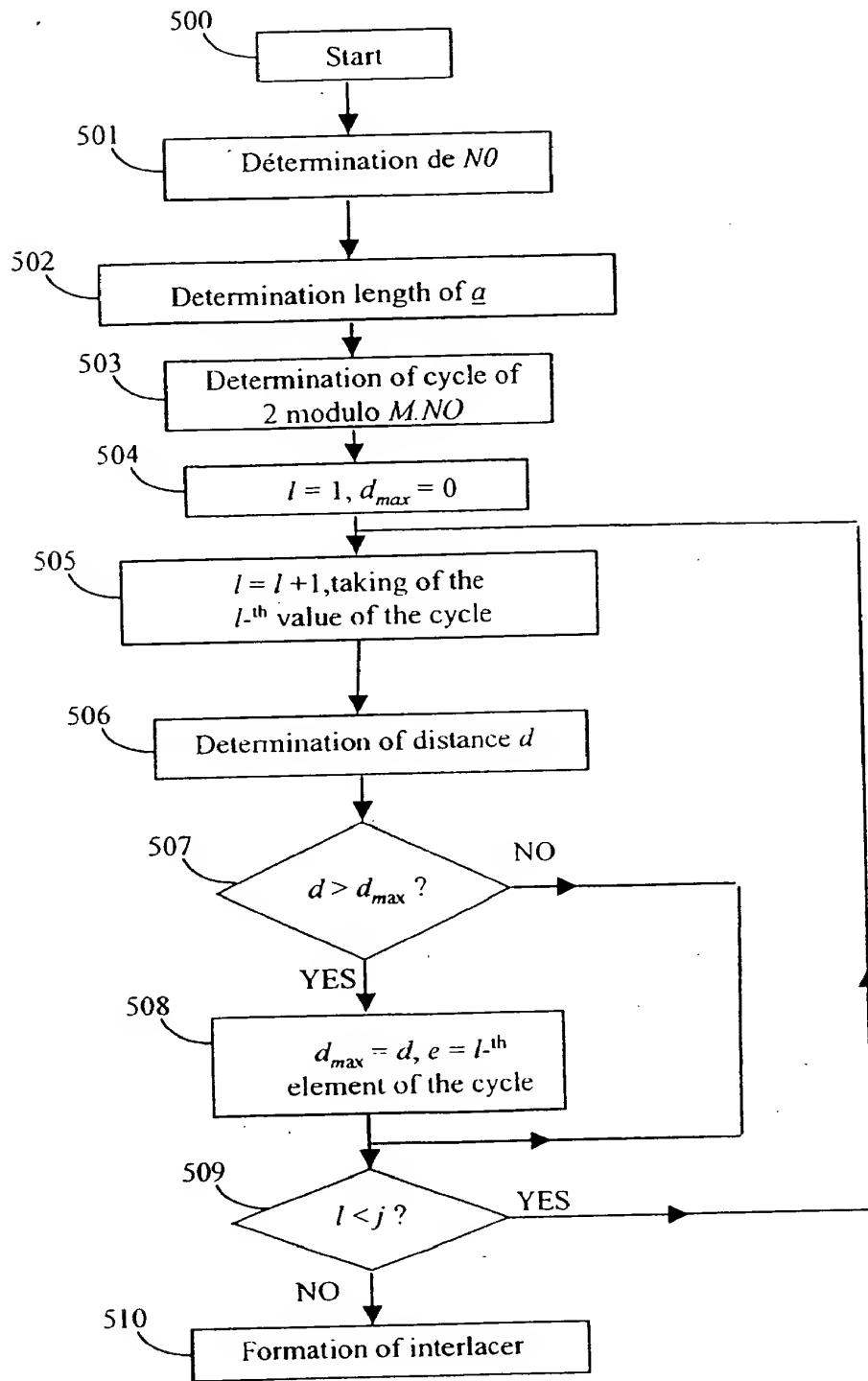


Fig.3

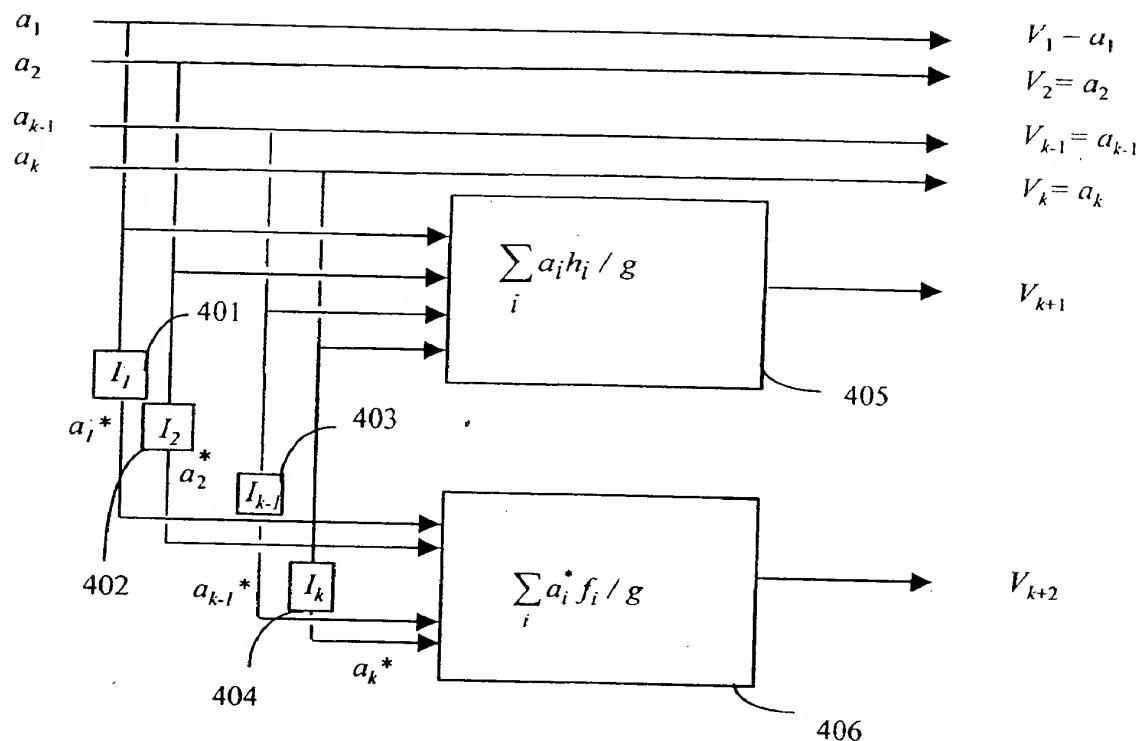
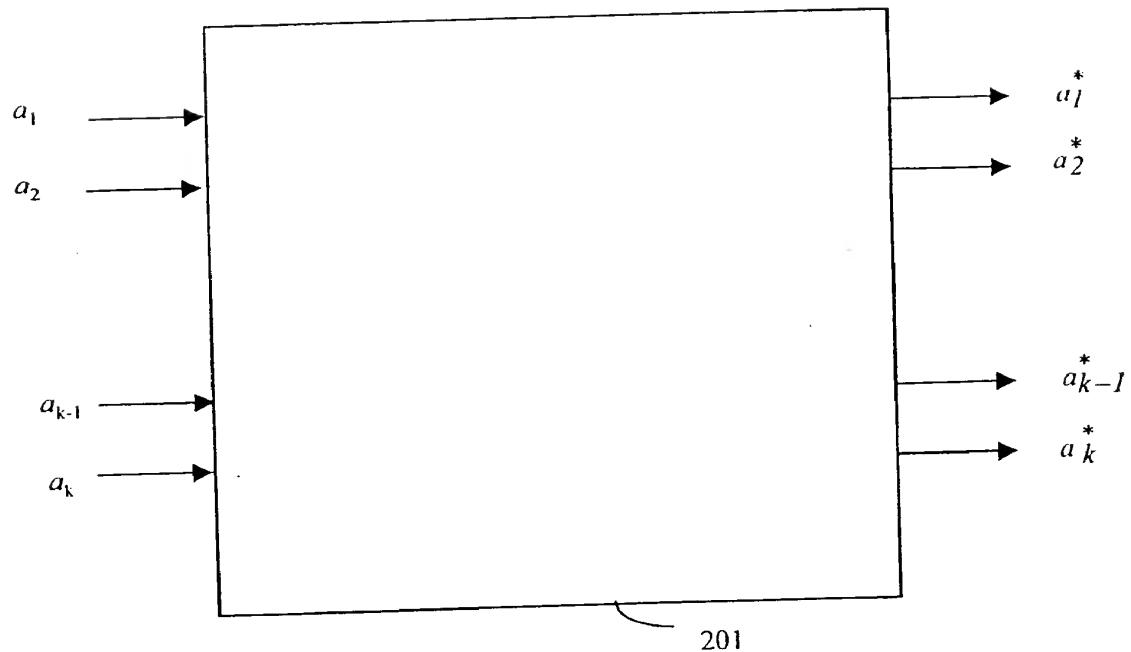


Fig.4



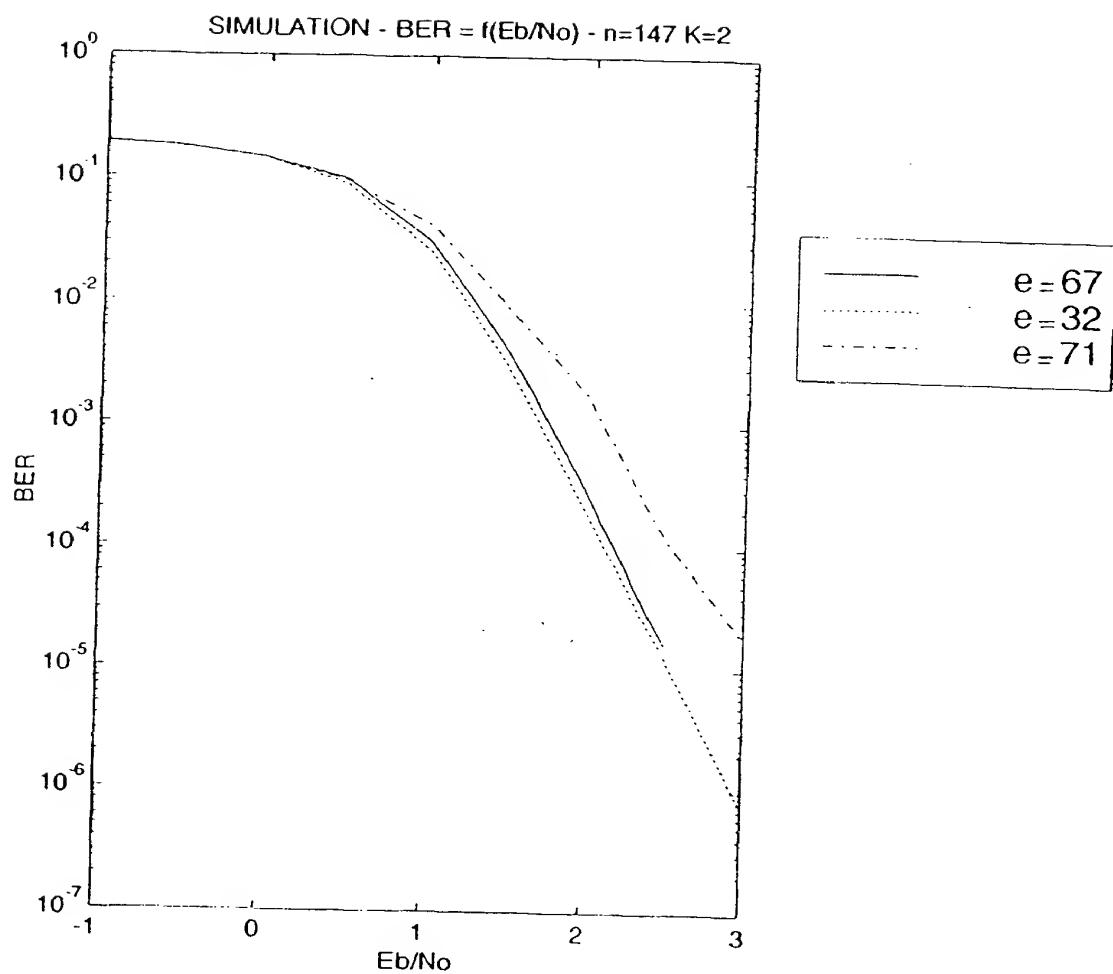
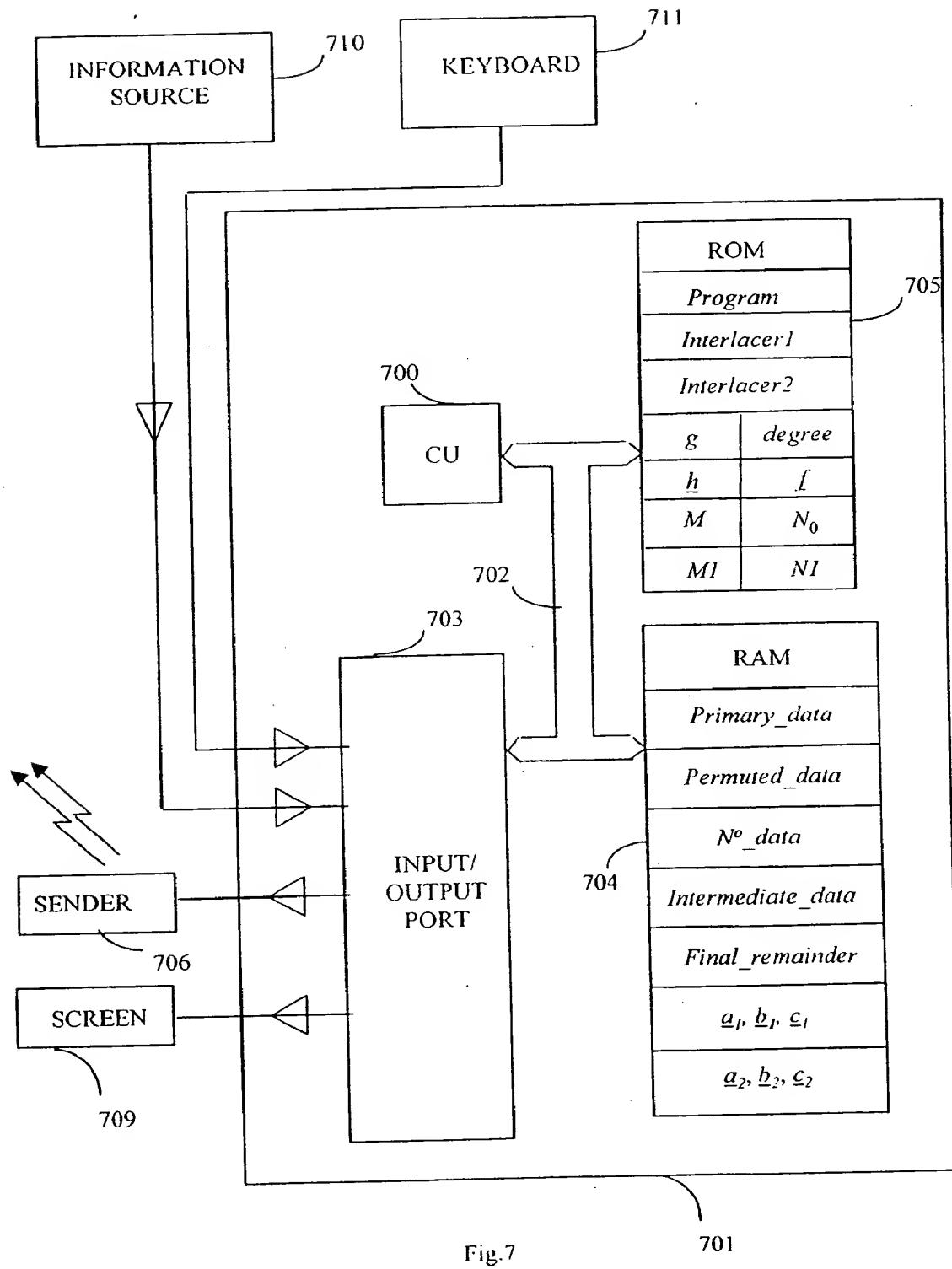


Fig.6



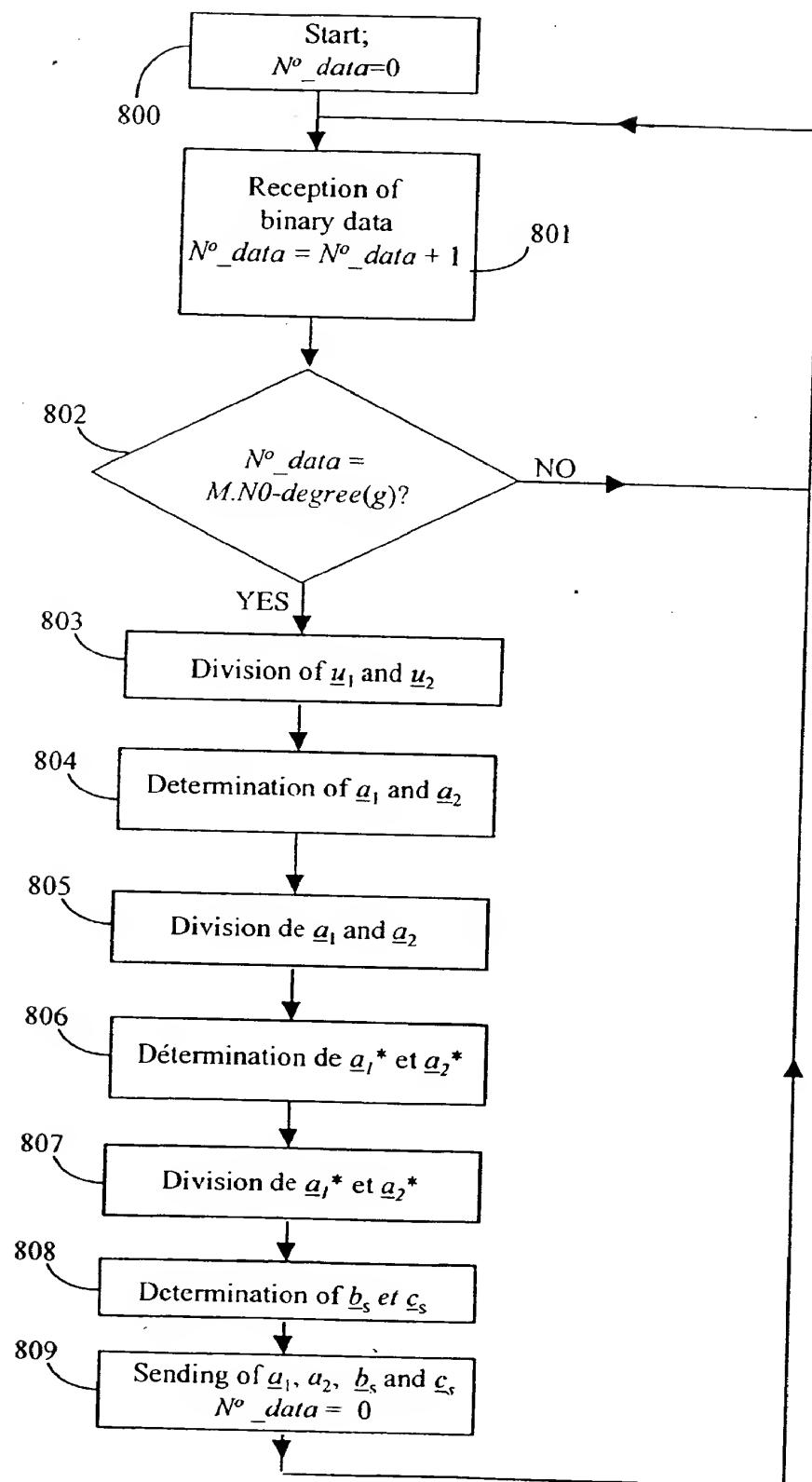
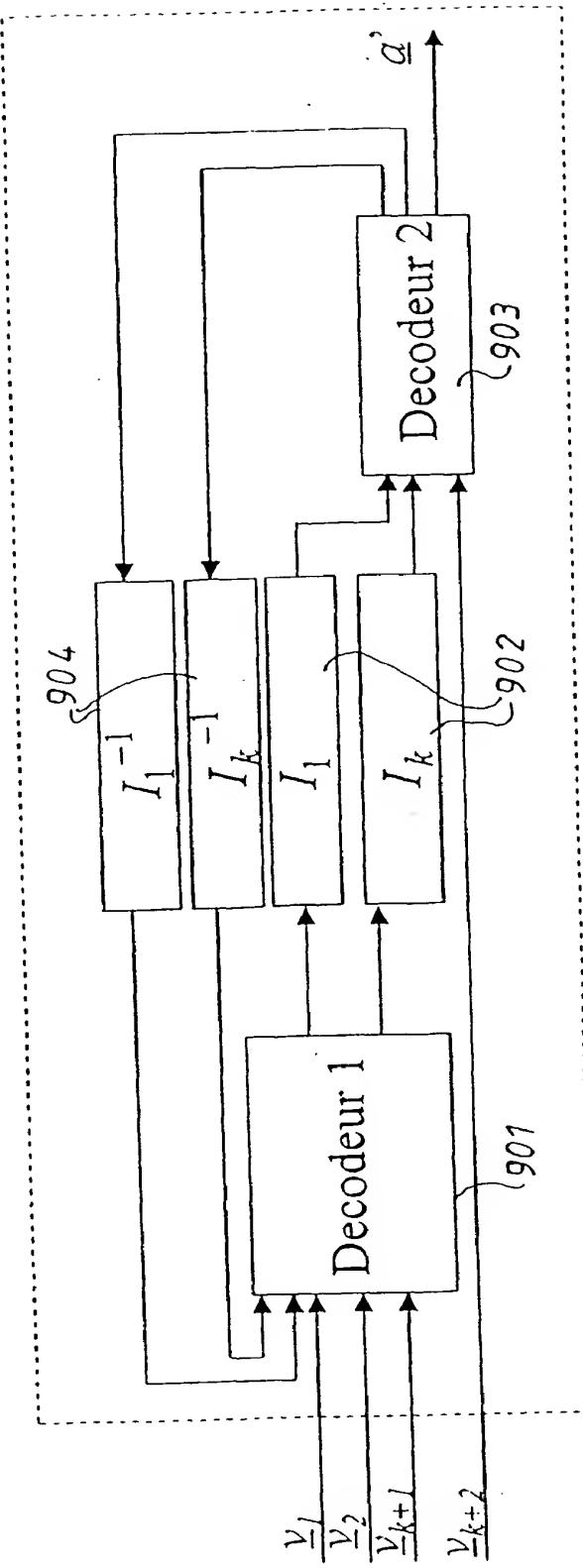


Fig.8

Fig. 9





European Patent
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EUROPEAN SEARCH REPORT

Application Number

EP 98 40 3283

DOCUMENTS CONSIDERED TO BE RELEVANT																		
Category	Citation of document with indication, where appropriate, of relevant passages	Relevant to claim	CLASSIFICATION OF THE APPLICATION (Int.Cl.6)															
X	US 4 567 594 A (DEODHAR SHIRISH P) 28 January 1986 * column 6, line 13 - line 59 *	19, 33	H03M13/00 H03M13/22															
X	US 4 907 233 A (DEUTSCH LESLIE J ET AL) 6 March 1990 * column 4, line 48 - column 5, line 23 *	18, 31, 32																
A	BERROU ET AL.: "Near Optimum error correcting coding and decoding : turbo codes" IEEE TRANSACTIONS ON COMMUNICATIONS, vol. 44, no. 10, October 1996, pages 1261-1271, XP000629465 IEEE Transactions on Communications paragraphes "Uniform interleaving" et "Nonuniform interleaving"	16, 17, 20, 30, 34																
A	DIVSALAR ET AL.: "Turbo codes for PCS applications" PROCEEDINGS OF THE INT'L CONFERENCE ON COMMUNICATIONS, vol. 1, 18 - 22 June 1995, pages 54-59, XP000532968 Seattle, US paragraphe "Interleaver design"		TECHNICAL FIELDS SEARCHED (Int.Cl.6)															
D, A	BARBULESU ET AL.: "Interleaver design for turbo codes" ELECTRONICS LETTERS, vol. 30, no. 25, 8 December 1994, pages 2107-2108, XP000501850 Stevenage, Herts, GB * the whole document *		H03M															
		-/-																
<p>The present search report has been drawn up for all claims</p> <table border="1"> <tr> <td>Place of search</td> <td>Date of completion of the search</td> <td>Examiner</td> </tr> <tr> <td>THE HAGUE</td> <td>8 April 1999</td> <td>Augarde, E</td> </tr> <tr> <td colspan="3">CATEGORY OF CITED DOCUMENTS</td> </tr> <tr> <td colspan="3"> X : particularly relevant if taken alone Y : particularly relevant if combined with another document of the same category A : technological background O : non-written disclosure P : intermediate document </td> </tr> <tr> <td colspan="3"> T : theory or principle underlying the invention E : earlier patent document, but published on, or after the filing date D : document cited in the application L : document cited for other reasons B : member of the same patent family, corresponding document </td> </tr> </table>				Place of search	Date of completion of the search	Examiner	THE HAGUE	8 April 1999	Augarde, E	CATEGORY OF CITED DOCUMENTS			X : particularly relevant if taken alone Y : particularly relevant if combined with another document of the same category A : technological background O : non-written disclosure P : intermediate document			T : theory or principle underlying the invention E : earlier patent document, but published on, or after the filing date D : document cited in the application L : document cited for other reasons B : member of the same patent family, corresponding document		
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EUROPEAN SEARCH REPORT

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DOCUMENTS CONSIDERED TO BE RELEVANT			CLASSIFICATION OF THE APPLICATION (Int.Cl.6)						
Category	Citation of document with indication, where appropriate, of relevant passages	Relevant to claim							
A	<p>BERROU ET AL.: "Frame oriented convolutional turbo codes" ELECTRONICS LETTERS, vol. 32, no. 15, 18 July 1996, pages 1362-1364, XP000625424 Stevenage, Herts, GB paragraphe " Theorem 1"</p>								
			TECHNICAL FIELDS SEARCHED (Int.Cl.6)						
<p>The present search report has been drawn up for all claims</p> <table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 33%;">Place of search</td> <td style="width: 33%;">Date of completion of the search</td> <td style="width: 34%;">Examiner</td> </tr> <tr> <td>THE HAGUE</td> <td>8 April 1999</td> <td>Augarde, E</td> </tr> </table>				Place of search	Date of completion of the search	Examiner	THE HAGUE	8 April 1999	Augarde, E
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THE HAGUE	8 April 1999	Augarde, E							
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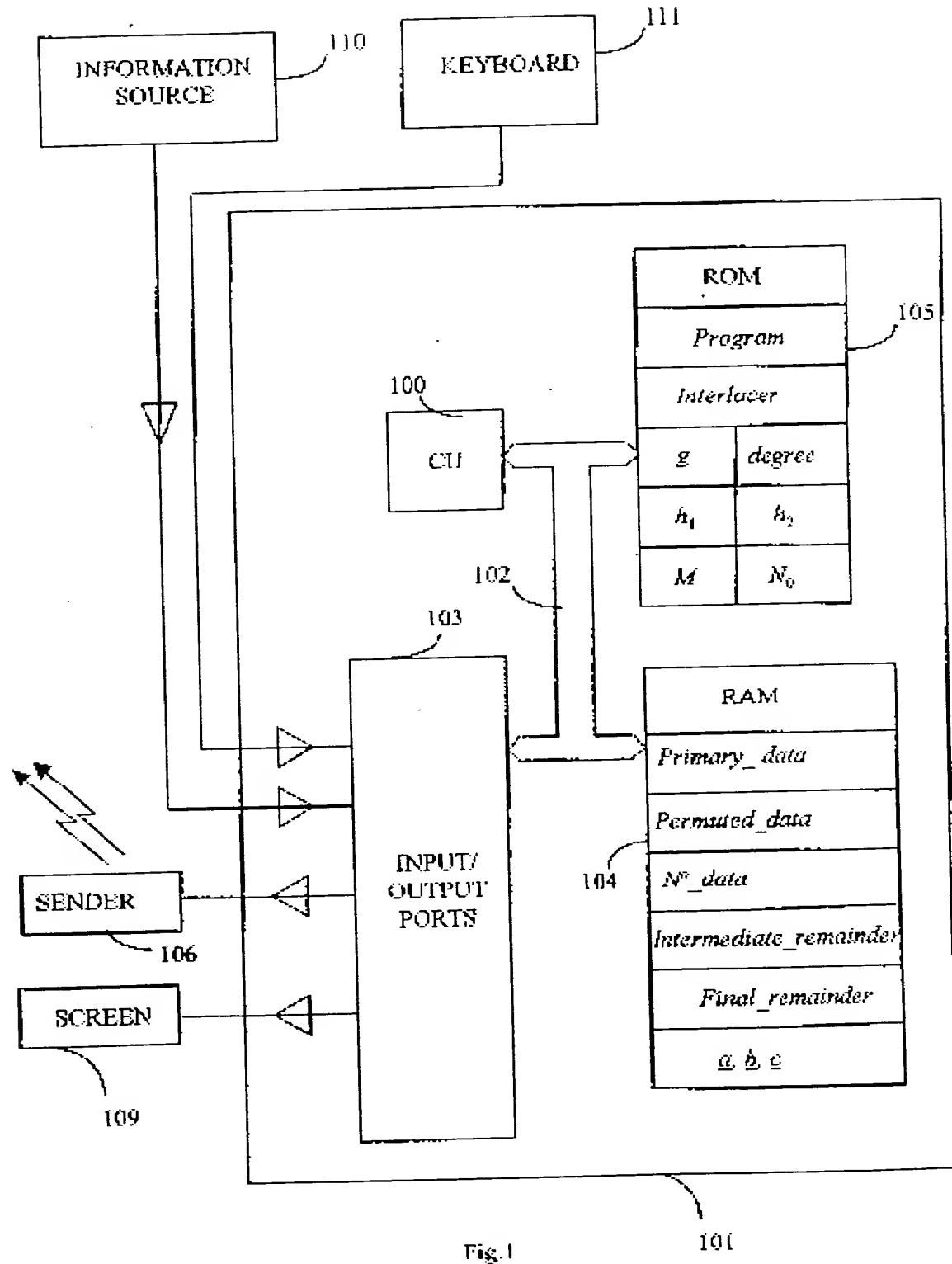
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ON EUROPEAN PATENT APPLICATION NO.

EP 98 40 3283

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08-04-1999

Patent document cited in search report		Publication date	Patent family member(s)	Publication date
US 4567594	A	28-01-1986	NONE	
US 4907233	A	06-03-1990	NONE	



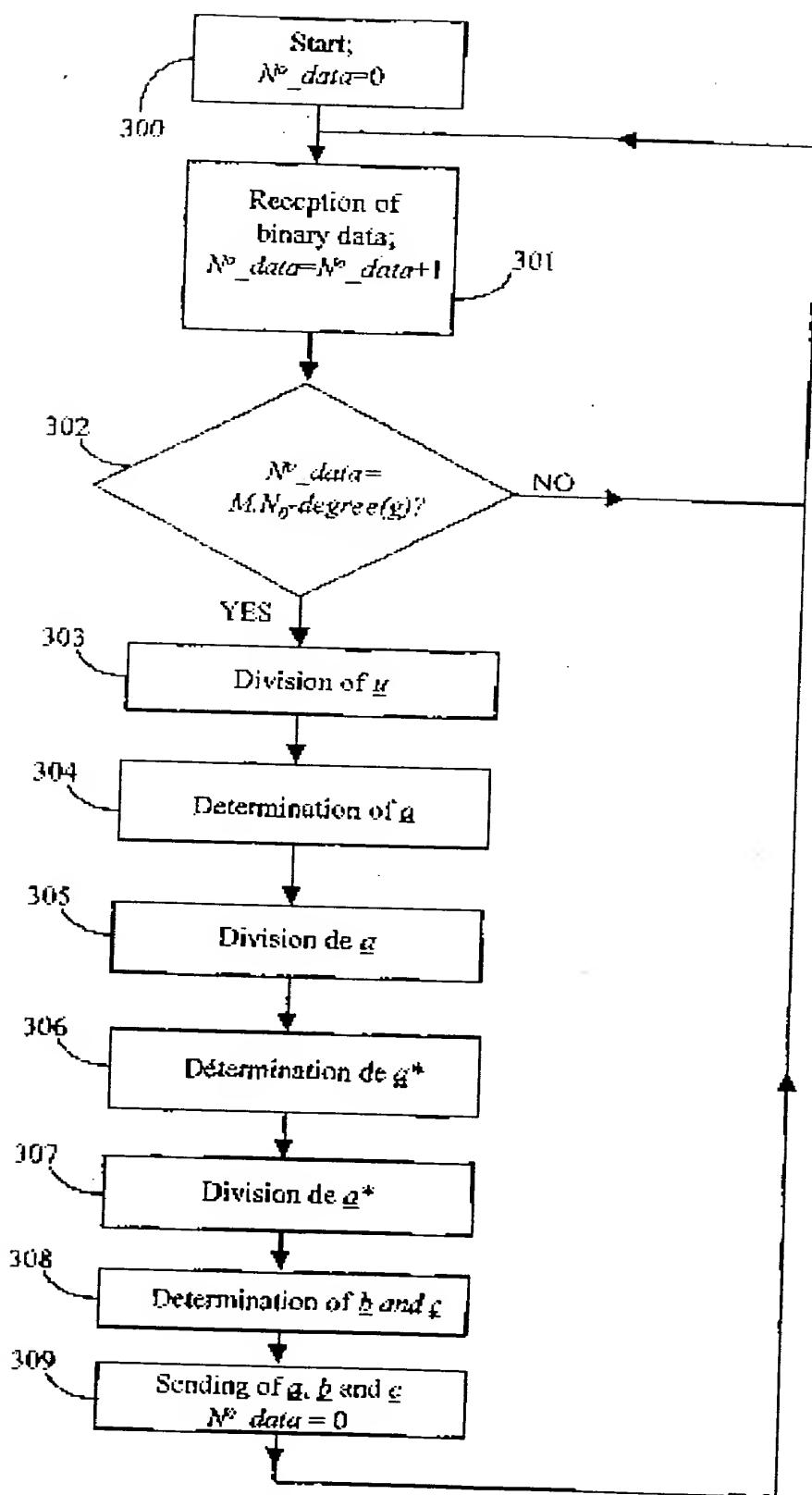


Fig.2

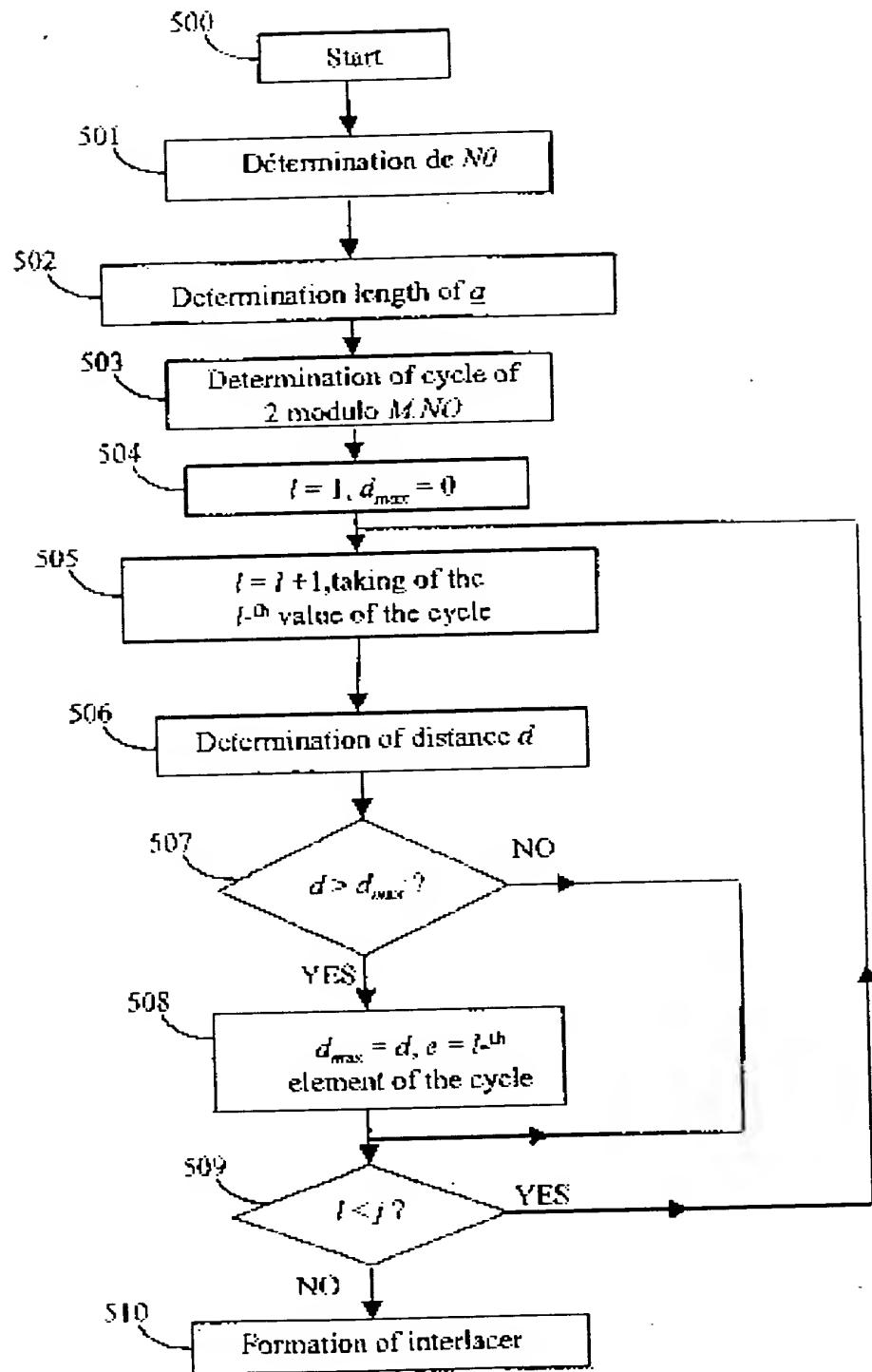


Fig.3

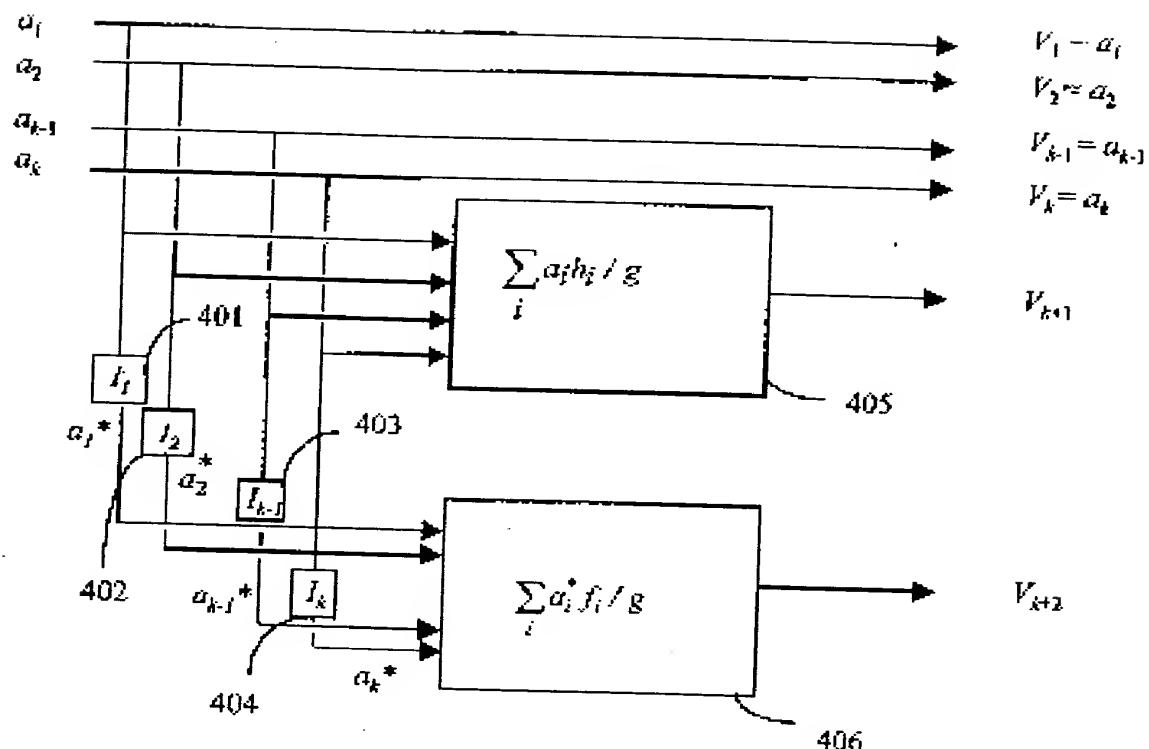
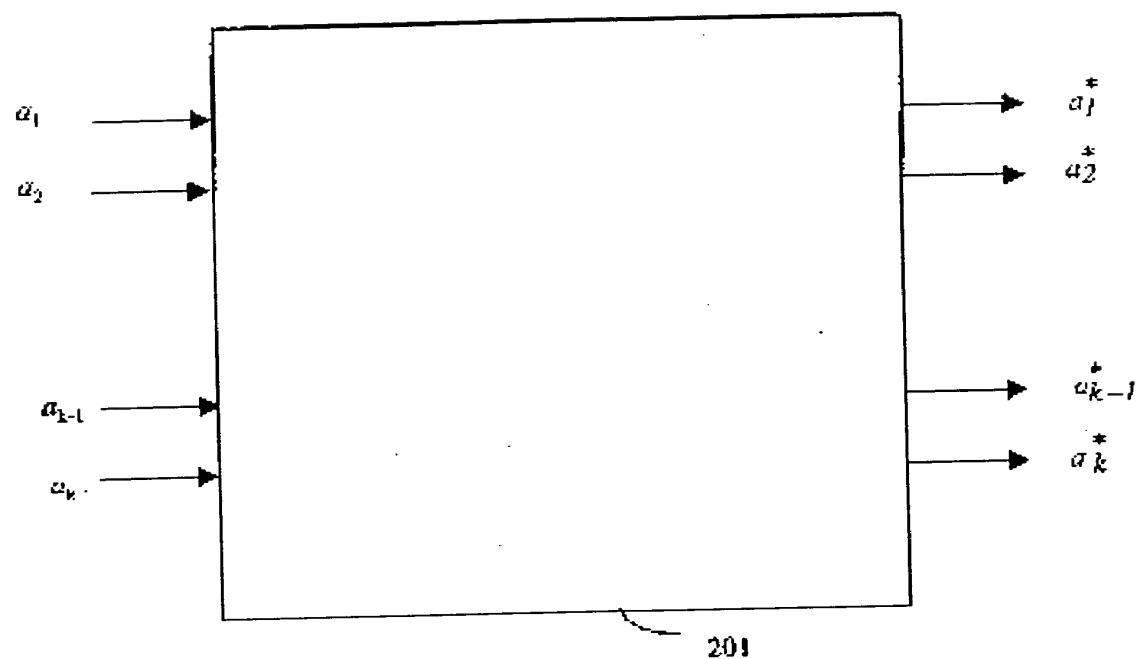


Fig.4



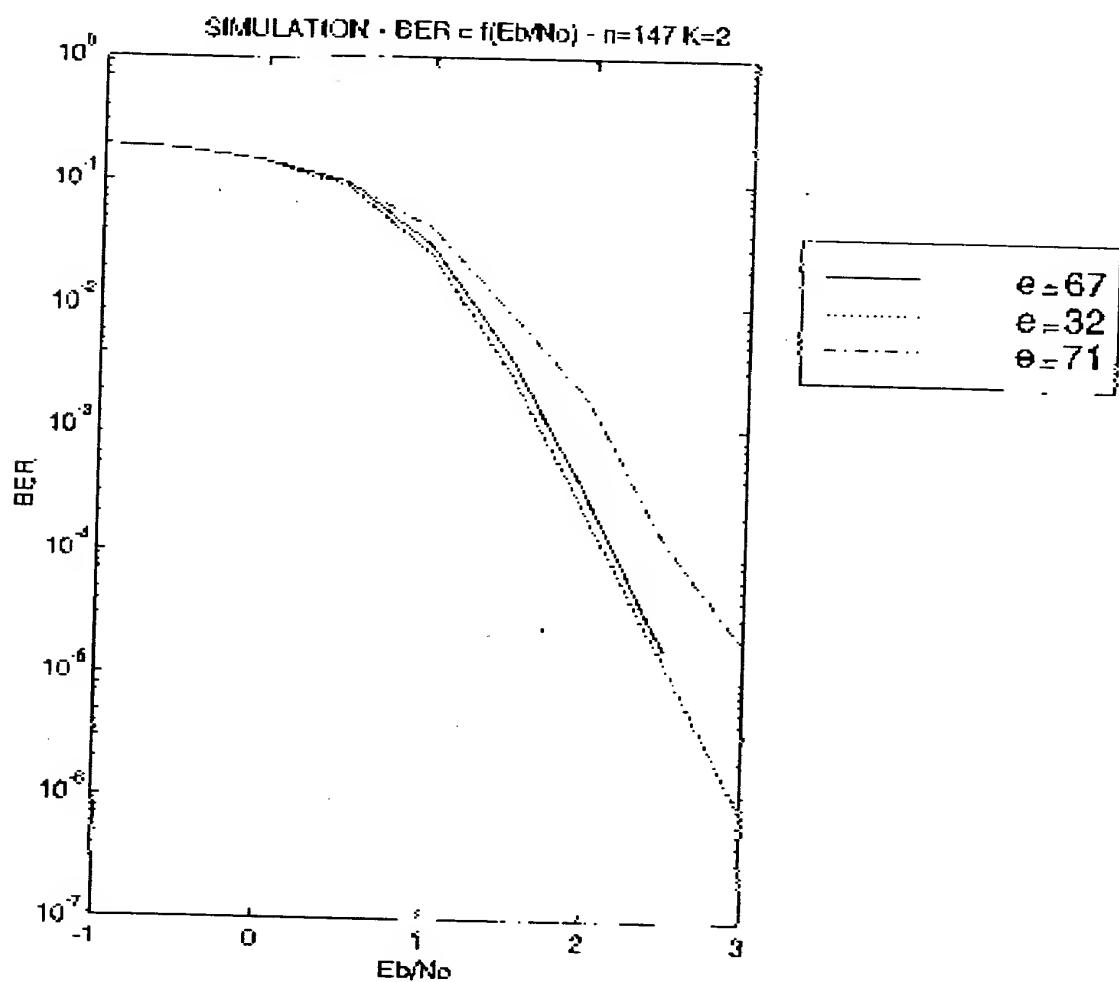


Fig.6

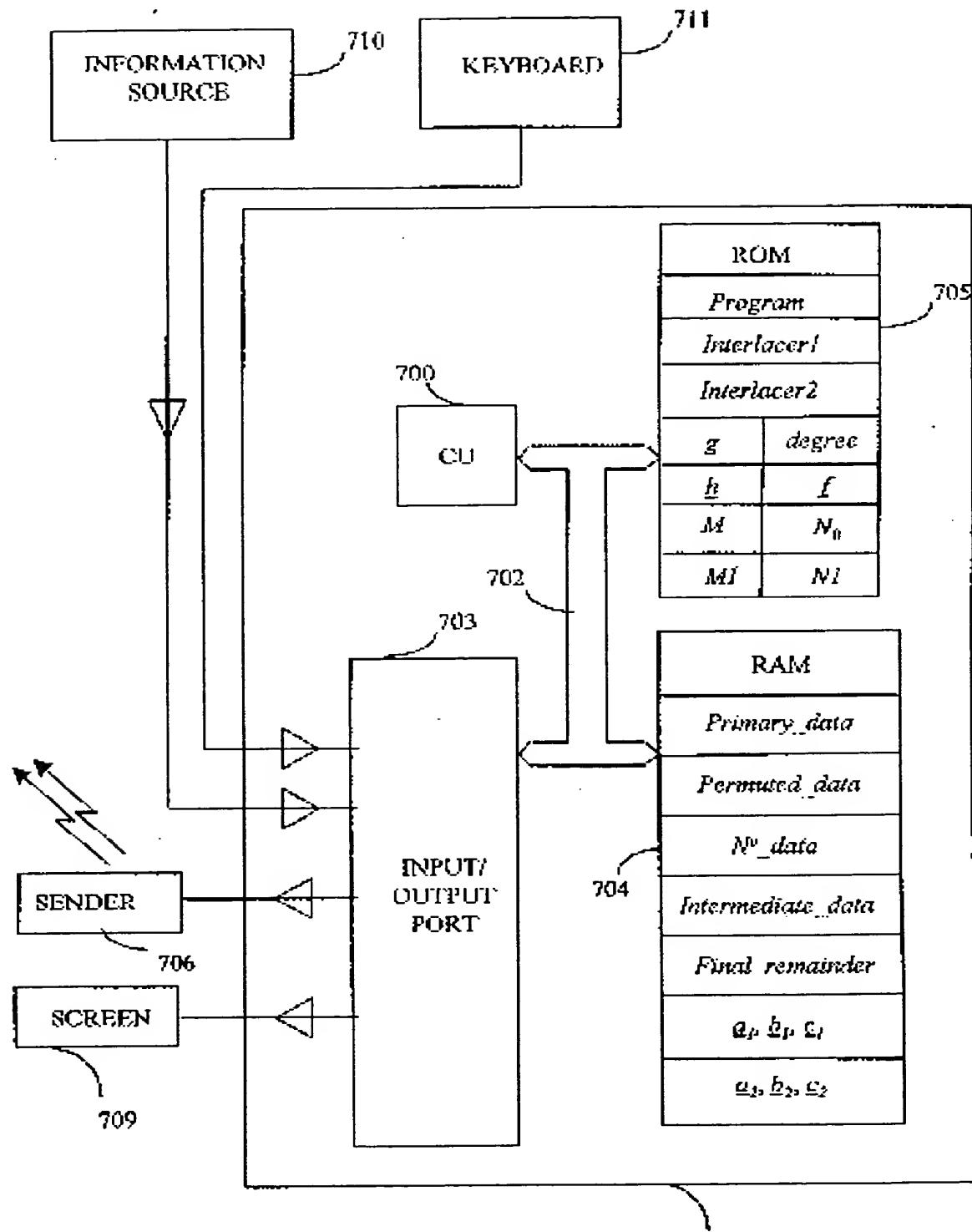


Fig. 7

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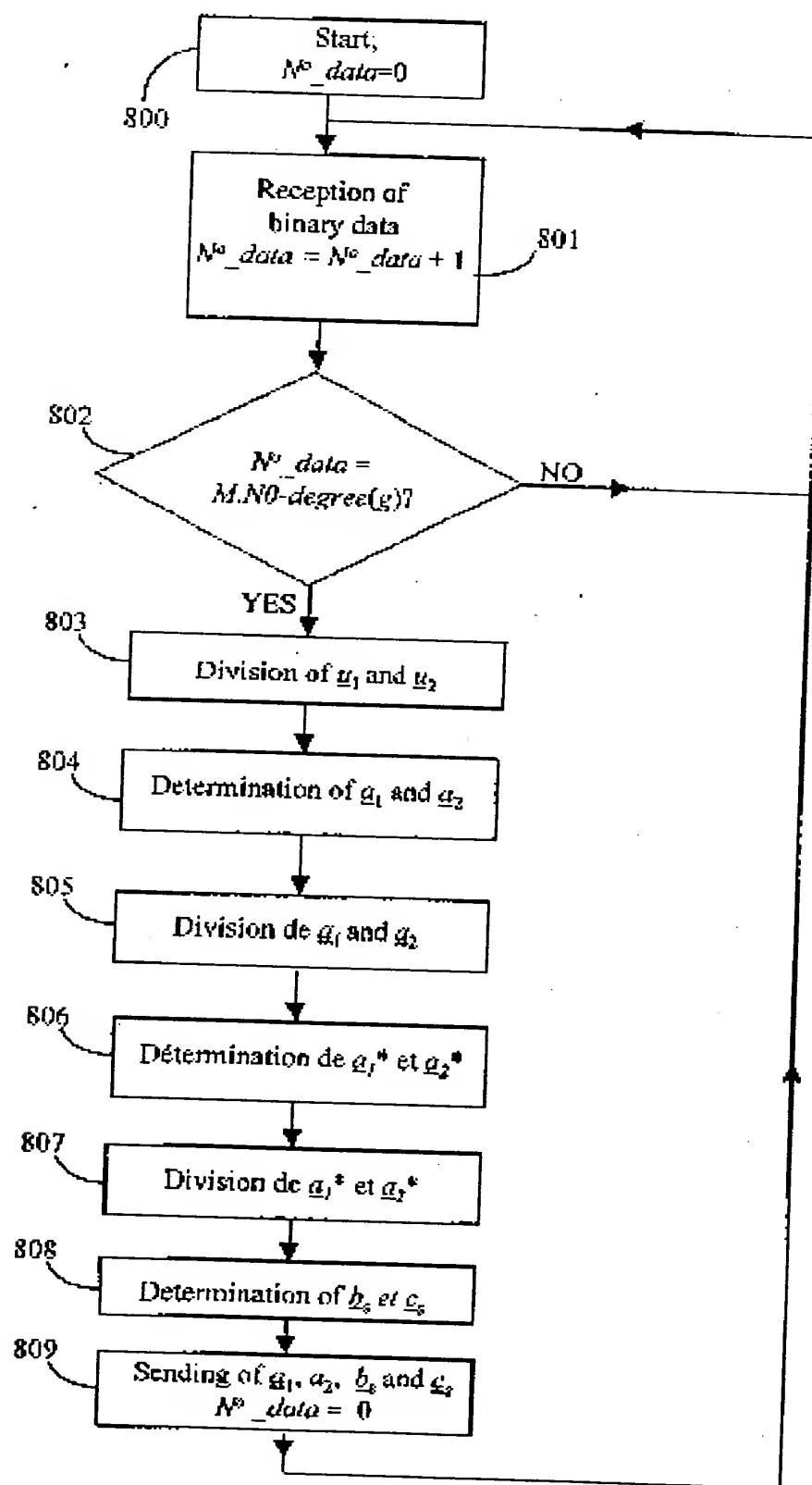
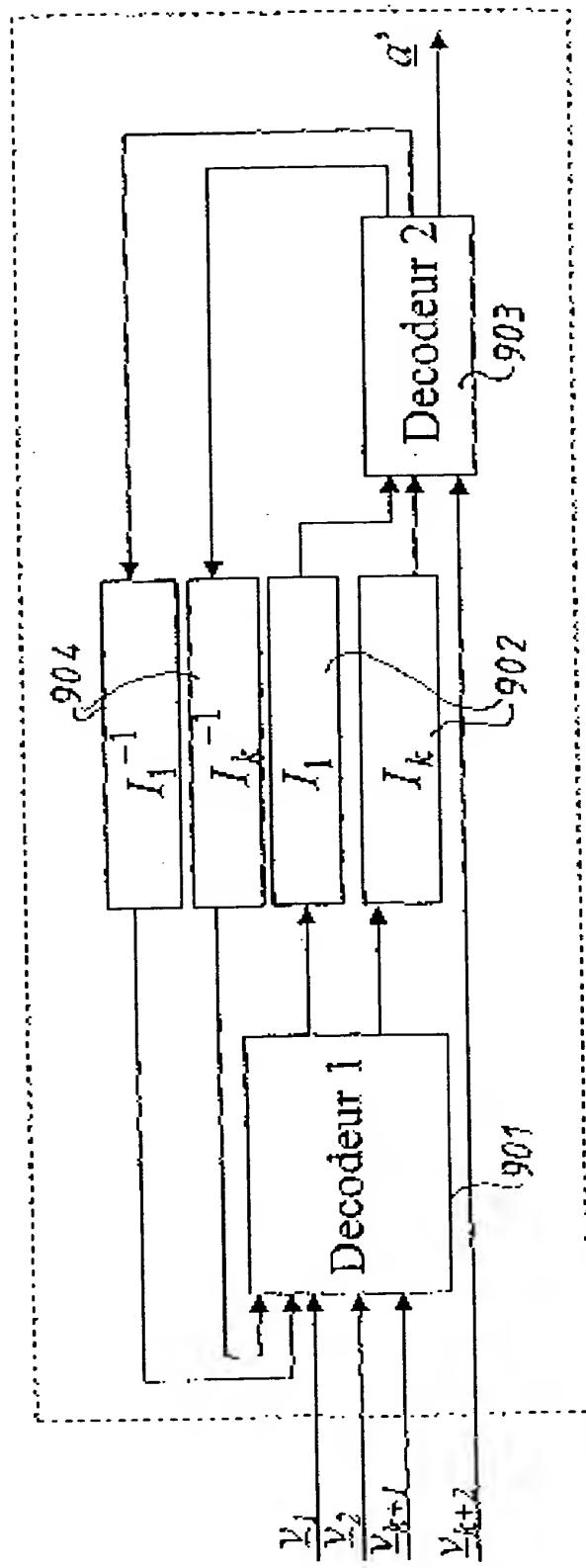


Fig.8

Fig. 9



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